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## New Tools for Decomposition of Sea Floor Pressure Data

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# New Tools for Decomposition of Sea Floor Pressure Data

A Practical Comparison of Modern and Classical Approaches

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## Abstract

In recent years more and more long-term broadband data sets are collected in geosciences. Therefore there is an urgent need of algorithms which semi-automatically analyse and decompose these data into separate periods which are associated with different processes. Often Fourier and Wavelet Transform is used to decompose the data into short and long period effects but these fail often because of their simplicity. In this paper we investigate the novel approaches Empirical Mode Decomposition and Sparse Decomposition for long-term sea floor pressure data analysis and compare them with the classical ones. Our results indicate that none of the methods fulfils all the requirements but Sparse Decomposition performed best except for computing efficiency.

*Keywords:* Time Series, Sea Floor Pressure Data, Fourier Transform, Wavelet Transform, Empirical Mode Decomposition, Sparse Decomposition

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## 1. Introduction

### 1.1. Motivation

Long-term monitoring of earth processes becomes more and more essential and indispensable as only long records will reveal small changes which

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5 may eventually have large societal impact in the near future. These pro-  
6 cesses encompasses geohazards like monitoring of potential landslides and  
7 volcanic activity but also processes related to earthquake precursors and cli-  
8 matic signals. In addition real-time observations of tectonic processes with  
9 high-precision GPS measurements and satellite based observations of the  
10 magnetic and gravity field of the earth give new insights into geological pro-  
11 cesses at local, regional and plate-size scales. As these signals are mostly  
12 small in amplitude and often buried in large-amplitude signals caused by  
13 other sources or only visible after major corrections to the field observations  
14 have been made it is a major challenge to separate the wanted from the  
15 unwanted signal components.

16 Broadband data acquisition is now very common as data storage ca-  
17 pacity is no major obstacle today and low power data acquisition with au-  
18 tonomous monitoring systems over considerably long time periods (i.e. years)  
19 in remote places like the deep ocean floor become more and more feasible.  
20 In addition large observational networks - either regionally only temporary  
21 like EarthScope (<http://www.earthscope.org/>) - or permanent like Nep-  
22 tune Canada (<http://www.neptunecanada.ca/>) or national or international  
23 geodetic GPS observation networks deliver continuously time series whose  
24 information content is not completely taken advantage of. All time series  
25 contain signal periods from short (several seconds) to long (several month  
26 to years); origin and cause of some signal components is sometimes quite  
27 well known (deterministic) as e.g. tides from various origins but in a lot of  
28 cases especially long-term changes are not well understood. In addition in-  
29 strumental behaviour like drift and effects of environmental changes severely  
30 alter the signal.

31 In earth science seismology has faced this problem for a long time which  
32 became even more pressing over the last decade during which the number  
33 of seismological stations increased accompanied by a tremendous increase of  
34 digital storage capacity and a rapid decrease in storage cost. In seismology  
35 robust methods were established to extract earthquakes from long data sets  
36 automatically and also detect phases and locate earthquakes. This highly au-  
37 tomated processing can be achieved because the characteristics of the signals  
38 are well-known and years of research have been spend until these algorithms  
39 were developed (Bormann, 2002).

40 Traditional tools for data analysis are mostly based on spectral analysis  
41 methods which are well established and available with a lot of software tools.  
42 However they tend to introduce unwanted effects especially at short periods

due to filters and finite length of time series. Also their requirement of a stationary time series is often not fulfilled in the case of long-term records. Therefore new data exploration tools are needed which enable us to separate the different signal components. These tools should be capable of analysing long time series efficiently and help to identify different signal contributions originating from different processes.

In this paper we present the results of time series analysis using four different methods. The times series analysed are sea floor pressure records from two different locations (details see section 1.2). The motivation for this investigation came from the fact that the sea floor pressure signal is dominated by a large deterministic tidal pressure signal but due to the high pressure resolution and a technically possible sampling interval of down to 2 seconds, small and short transient signals can be observed. Superimposed on these tides are also long-period transient changes, associated with tectonic and/or oceanographic phenomena but also short period signals originating from local or teleseismic events. The problem was and still is to separate the deterministic from the small-amplitude non-deterministic signals. Traditional tidal analysis methods as described e.g. in Pawlowicz et al. (2002) and available as Matlab<sup>®</sup> toolbox (<http://www.eos.ubc.ca/~rich/>) do not always fulfil the requirements.

We tested four methods in total: the traditional (1) Harmonic Decomposition, (2) Wavelet Decomposition, (3) Empirical Mode Decomposition (EMD) and a novel approach (4) Sparse Decomposition. The last two methods used are rather new and their potential use in time series analysis needs still to be explored. All times series were analysed in the same way with the four methods. After a short description of the methods we present the results and compare the results with respect to their capability of signal decomposition.

## 1.2. Data

We used four data sets to test the four methods for time series decomposition. The first data set (SYN) is a synthetic data set which is composed of a tidal signal calculated with a published Matlab<sup>®</sup>-script (Pawlowicz et al., 2002), a long-term ramp function and two short-period events. In addition noise with an RMS of 49.16 *Pa* is added. A step in the middle of the time series simulates a tectonic or oceanographic event. The second time series (MAR) consists of sea floor pressure observations from the Logatchev Hydrothermal Field, located at the Mid-Atlantic Ridge (Gennerich and Villinger, 2011). Sea floor pressure measurements at this site were made

in order to monitor the magmatic and hydrothermal activity of the field which might express themselves as changes in sea floor pressure either due to subsidence or uplift or by tremor-like signals related to hydrothermal processes in the subsurface. The third and fourth records (CORK1 and CORK2) come from a so called CORK (Becker and Davis, 2005) installed at the sea floor off Vancouver Island. A CORK (Circulation Obviation Retrofit Kit) is a sea floor installation which is placed on top of a drill hole and isolates the hydrological - and pressure - regime inside the drill hole from the ocean. The main purpose of this installation is the long-term monitoring of pressure signals inside the drill hole in order to identify either slow earthquakes i.e. long period changes in the sub sea floor stress field or the response of the formation to seismic events which reveal the hydrological and permeability structure of the oceanic crust (e.g. Davis et al. (2011)). At every CORK installation sea floor pressures are recorded in addition to the downhole pressures to provide a local pressure reference signal.

In all cases (MAR, CORK1 and CORK2) pressures were recorded with high-resolution absolute pressure sensors (<http://www.paroscientific.com/uwapp.htm>) with a resolution of 7 Pa which is about 7 mm equivalent water height change. More details on location and sample intervals can be found in table 1.

Table 1: Details of the data sets used in the tests.

Data set	Start	End	Duration [days]	$\Delta t$ [min]	Position	
					Latitude	Longitude
SYN			41.7	60	48° 26'N	128° 43'W
MAR	01.05.2008	31.05.2008	30	2	14° 45'N	44° 5' W
CORK1	26.06.2003	15.09.2005	1046	10	48° 26'N	128° 43'W
CORK2	11.09.1996	15.09.2005	3292	60		

## 2. Methods for Decomposing

In this section we discuss the methods used to decompose the data. These are

### 1. Harmonic Decomposition

- 104 2. Wavelet Decomposition
- 105 3. Empirical Mode Decomposition
- 106 4. Sparse Decomposition

107 The classical methods Harmonic and Wavelet Decomposition are well known.  
108 Therefore we have chosen them to have a comparison for the new methods  
109 Empirical Mode Decomposition and Sparse Decomposition.

110 All methods have in common that they seek for a new representation,  
111 as a superposition of several *patterns*, of the data, in most cases by basis  
112 transformation.

### 113 2.1. Harmonic Decomposition

114 The Harmonic Decomposition uses the Fourier Transform with its efficient  
115 implementation as Fast Fourier Transform (FFT). It is known since almost  
116 fifty years and used in many data processing routines. The basic idea is to  
117 transform the given time signal into the frequency space. In other words we  
118 are looking for a representation with sinusoidal pattern with different frequen-  
119 cies. We refer to [Gröchenig \(2001\)](#) as a reference for a detailed introduction  
120 to Fourier Analysis. A much shorter introduction of the Fourier Transform  
121 is given in nearly every book about signal analysis, like [Stark \(2005\)](#).

122 Decomposition of our time series with the help of Fourier Analysis starts  
123 with a FFT. As we know the frequencies and amplitudes of the tides from  
124 theoretical considerations and from observations, we can decompose the data  
125 into several components and remove the unwanted and deterministic ones.  
126 The remaining spectrum is transformed into a time series which contains  
127 only the non-tidal components.

### 128 2.2. Wavelet Decomposition

129 Another technique for decomposing the data is the Wavelet Decompo-  
130 sition which uses the Wavelet Transform. It is not as old as the Fourier  
131 Transform but it is also known very well. Like the Fourier Transform, it  
132 transfers the given time signal in another space. This time the basis vectors  
133 are scalings and translational displacements of a basic pattern, called *mother*  
134 *wavelet*, hence in this space the coefficients encode when an effect is mea-  
135 sured and how long this effect was. Therefore we can again decompose our  
136 data in features of a short and long period of time. Just like for the Fourier  
137 Transform there are fast implementations for the Wavelet Transform. For  
138 further informations about wavelets see [Louis et al. \(1997\)](#) or [Stark \(2005\)](#).

139 First of all we have to choose the mother wavelet and a number of levels  
 140 in which we want to decompose our signal. Unlike the Fourier Transform  
 141 where the orthogonal functions are pre-defined, we have to choose the mother  
 142 wavelet a priori. If we have extra knowledge about the data, we can improve  
 143 the results by choosing a wavelet which is 'similar' to the data or rather the  
 144 features we would like to extract. In our case the Wavelets *Daubechies 10* -  
 145 *Daubechies 40* (often abbreviated by *db10* and *db40*) fit the tidal components  
 146 very well. After performing the Wavelet Transform with these wavelets, we  
 147 obtained the best results by using *db40*, which is shown in figure 1.

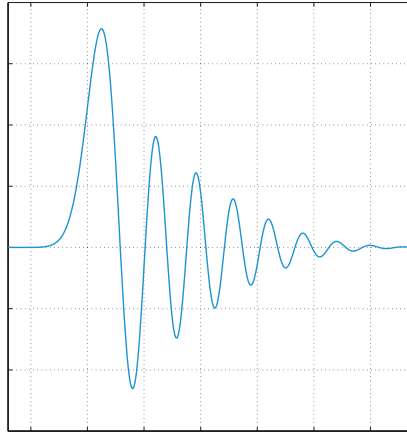


Figure 1: Wavelet *db40* (scaling function)

### 148 2.3. Empirical Mode Decomposition

149 The third method we would like to introduce is the Empirical Mode De-  
 150 composition and its enhancement the Ensemble Empirical Mode Decomposi-  
 151 tion (EEMD). The EMD is a new method, invented by [Huang et al. \(1998\)](#),  
 152 for decomposing a time signal. Since it is not as basic as the Fourier and  
 153 Wavelet Transform, we present the algorithm here. The idea is to decompose  
 154 the given time signal into a finite number of Intrinsic Mode Functions (IMF),  
 155 which are functions which satisfy two conditions:

- 156 1. The number of extrema and the number of zero crossings must differ  
 157 at most by one.
- 158 2. The mean value of the upper and lower envelope is zero at any time,  
 159 where the upper envelope is computed by interpolating the maxima  
 160 and the lower envelope by interpolating the minima.



161 The task of the EMD is to find these IMF's and is done by the following  
 162 *sifting process*, also shown in figure 2.

- 163 1. Find all extrema of the given data.
- 164 2. If the number of extrema is one or less, we have found all IMFs and  
 165 terminate the algorithm.
- 166 3. Compute the upper and lower envelope by interpolation the maxima  
 167 and minima and the mean of these.
- 168 4. If the mean value is zero, we have found an IMF. Start the sifting  
 169 process again with the data subtracted by this IMF. Otherwise start  
 170 the sifting process again with the data subtracted by the mean.

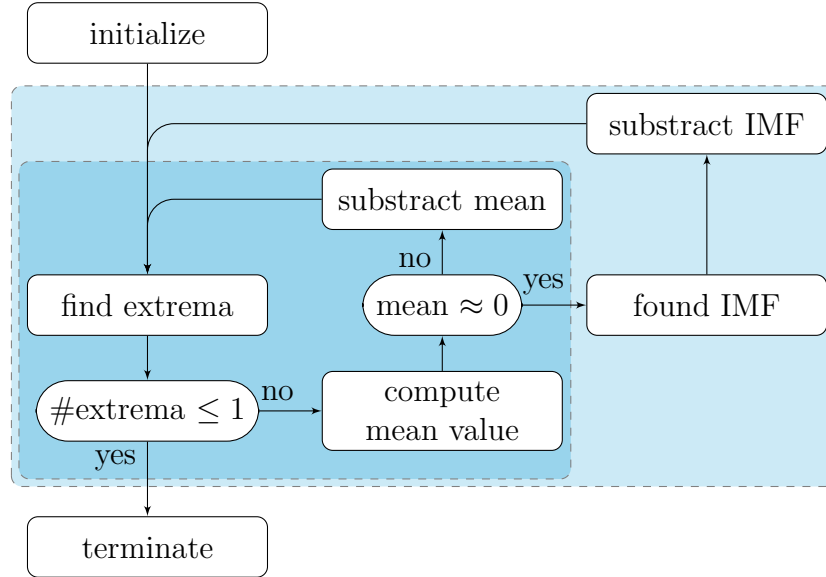


Figure 2: The algorithm of the EMD. The coloured areas represent the loops of the algorithm.

171 Also the EMD can be seen as a basis transformation, but this time the  
 172 patterns, which are the IMFs, depend on the data.

173 As we have seen we have done no a priori choices but choosing the in-  
 174 terpolating scheme, which is predefined by cubic splines. Since abstracting  
 175 an IMF reduces the number of extrema this algorithm terminates for every  
 176 finite time signal. A disadvantage of this method is that it is empirical and  
 177 has no solid theoretical foundation. Compared to the Fourier and Wavelet

178 Transform the computing effort to decompose the data by EMD is higher  
 179 but still tolerable. A detailed introduction to EMD is given in [Huang et al.](#)  
 180 [\(1998\)](#).

181 A challenge in decomposing time series is to prevent *mode mixing*. Phe-  
 182 nomena of similar time scale should be in the same mode (here: IMF) and  
 183 vice versa phenomena with a totally different scale are expected to have a  
 184 different mode. For this purpose Wu and Huang suggested in 2009 a noise  
 185 assisted data analysis method, called EEMD ([Wu and Huang, 2009](#)). For  
 186 a given signal white noise is added to the signal and then decomposed us-  
 187 ing the EMD. At the end - after numerous trials - we take the mean of the  
 188 IMF's. "By adding finite noise, the EEMD eliminated largely the mode mix-  
 189 ing problem and preserve physical uniqueness of decomposition. Therefore,  
 190 the EEMD represents a major improvement of the EMD method." ([Wu and](#)  
 191 [Huang, 2009](#)). Of course this is more time consuming than the usual EMD  
 192 and we have to check if this is worthwhile in our application or not.

#### 193 2.4. Sparse Decomposition

The last method we would like to present is the Sparse Decomposition.  
 We assume that the given data is a superposition of some processes. Then  
 we can find these by minimizing the residual

$$\|\vec{k}_1 x_1 + \dots + \vec{k}_n x_n - \vec{y}\|_2,$$

where  $\vec{k}_1, \dots, \vec{k}_n$  are the possible patterns. Writing  $\vec{k}_1, \dots, \vec{k}_n$  as the columns  
 of a matrix  $K$ , then this is the same as

$$\|K\vec{x} - \vec{y}\|_2.$$

194 The Fourier and the Wavelet Transform can also be written as such a mini-  
 195 mization problem by choosing the patterns as harmonics or wavelets respec-  
 196 tively. The advantage compared to the Fourier and Wavelet Transform is that  
 197 we are not restricted to only one basis to find our decomposition, but we can  
 198 incorporate several bases, which is called a *dictionary*. For our purposes  
 199 we have chosen a dictionary with translational displacements and scalings  
 200 of the pattern in figure 3, hence we combine the capability of the Fourier  
 201 and Wavelet Transform. Furthermore, we can also add any other pattern to  
 202 increase the physical meaning of the decomposition.

We are looking for a solution which has a small residual and is *sparse*,  
 i.e. it uses only a few patterns. A decomposition of the data into only a few

patterns is likely to have physical meaning, especially when the patterns are chosen according to physical effects. This can be achieved by minimizing

$$\frac{1}{2}\|K\vec{x} - \vec{y}\|_2^2 + \alpha\|\vec{x}\|_1,$$

see Daubechies et al. (2004). The last term  $\|\vec{x}\|_1$ , called *penalty term*, is the sum of the absolute values of  $\vec{x}$ . The notion of Sparse Decomposition is also investigated in an applied manner in Chen et al. (1999).

For our application we have chosen the algorithm Regularized Feature Sign Search (RFSS), invented by Jin et al. (2009) and based on Lee et al. (2007), to minimize these functional.

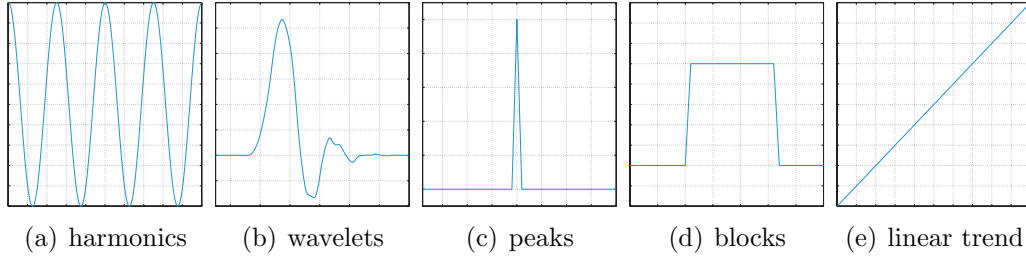


Figure 3: The chosen dictionary which contains harmonic waves, a wavelet basis, a peak basis, blocks and a linear trend.

The choice of the dictionary is an advantage and disadvantage at the same time. If we have special knowledge of our data, like in most cases, we can improve the decomposition by choosing 'good' pattern. On the other hand an algorithm which requires many input parameters is often difficult to handle. A disadvantage is that the algorithm is much more demanding and complex compared to the other methods. We will see later on that this is worthwhile.

Further information and the full algorithm is given by Jin et al. (2009).

### 3. Results

In this section we present and discuss our results. First of all we have to mention that the used data is preprocessed by subtracting the mean value, so the important features are emphasized.

Our results for Harmonic and Wavelet Decomposition are obtained by using Matlab<sup>®</sup>'s functions `fft` and `wavedec` respectively. For EMD and EEMD

we have used the algorithms by [Rilling \(2007\)](#) and [Wu \(downloaded 04/2011\)](#). The RFSS implementation, used for the Sparse Decomposition, was according to [Schiffler \(2009\)](#). All algorithms can be found on the world wide web, see our references.

The tidal extraction from the data sets is done very well by all algorithms, hence this does not distinguish the methods and is not discussed in the following.

### 3.1. *Decomposition of SYN*

The results of the decomposition of the synthetic data are shown in figure 4. Since it is a synthetic data set we can compare the computed decomposition by the real one to evaluate their quality.

As we see the methods' ability to decompose this data varies substantially. Harmonic and Wavelet Decomposition are able to decompose the data into features of three different types. The noise and the short effects are in the same component. The methods EMD and EEMD are not able to extract the high frequency features from the signal. All algorithms were able to separate the long-term effects from the rest but failed to distinguish between the trend and the step.

Harmonic and Wavelet Decomposition as well as the Sparse Decomposition correctly detect the short time features as well in time as in amplitude. Only large boundary effects in the results obtained by Harmonic and Wavelet degrade their quality. Methodically we can not obtain boundary effects in the results of the Sparse Decomposition, since we have chosen our dictionary to contain local and global pattern. Hence local features do not have to be reconstructed by global pattern. Additionally the RFSS is not based on filtering, which often causes boundary effects. Overall the Sparse Decomposition performs best in detecting the short time features.

The last aim was to extract the long time effects. All algorithms perform quite well, but again the boundary effects degrade the Harmonic and Wavelet results. Sparse Decomposition is capable of extracting the trend and the step very well whereas EMD and EEMD reproduce only the trend satisfactorily.

### 3.2. *Decomposition of MAR*

The next data set to test is the one from the Mid-Atlantic Ridge and the results can be seen in figure 5. This time all algorithms provide a good decomposition into the short-, medium- and long-period features. Only the Sparse Decomposition is able to extract also the noise from the short-period

259 components. There are just a few peaks visible in the short-period decom-  
 260 position by Harmonic Decomposition and EMD which are probably aliased  
 261 local earthquake signals. These are also extracted very well by the Sparse De-  
 262 composition. The short-period features given by Wavelet show again some  
 263 boundary effects. The decomposition by the EEMD has a basic noise level  
 264 which is much too high. This is a result of the white noise added in every  
 265 step of the algorithm but which is clearly not faded away with 100 runs of  
 266 the EMD.

267 The trend and long-term feature extraction of the five methods are all  
 268 nearly the same. In all cases pressures decrease initially over the first week  
 269 and then increase by about  $0.4 \text{ kPa}$  over the rest of the time window. The  
 270 Wavelet results differ from the others by significant boundary effects.

### 271 3.3. *Decomposition of CORK1*

272 The results of the third data set, CORK1, are given in figure 6. This time  
 273 every method is again capable to decompose the data into the three main  
 274 features. In this data set there are two short time effects whose amplitudes  
 275 are a lot higher than the amplitudes of the other effects so we have also  
 276 showed the short period effects zoomed in.

277 The similarity between the short period features detected by Harmonic  
 278 and Wavelet Decomposition is worth mentioning. The EMD and EEMD de-  
 279 tect these features very similar in time but differ in detecting the amplitude.  
 280 Also the EEMD is not able to detect short period features with a small am-  
 281 plitude since the added noise prevents this. The Sparse Decomposition is  
 282 able to detect these features as well and separates them additionally from  
 283 the noise.

284 The trends detected by all methods are again quite similar. Only the  
 285 Wavelet trend has huge boundary effects. The behaviour of Harmonic De-  
 286 composition at the boundary could be interpreted as a boundary effect, but  
 287 we guess this is not the case, since Sparse Decomposition predict the same  
 288 and is methodically unaffected by boundary effects. The same behaviour can  
 289 be obtained from the EEMD's trend.

### 290 3.4. *Decomposition of CORK2*

291 For the last data set the results are given in figure 7. Since this is a  
 292 long data set and the sampling interval is only  $60 \text{ min}$  we focus on the long  
 293 period effects. On the other hand we can not expect short time features  
 294 with a shorter duration than  $60 \text{ min}$ , like earthquakes, to appear in this data

295 set, hence the short time components obtained from this data set has to be  
296 interpreted very carefully.

297 Like with the dataset SYN, which sampling interval was also 60 *min*,  
298 EMD and EEMD are not capable to decompose the features with higher  
299 frequencies than the tides. Contrary this is done very well by Harmonic,  
300 Wavelet and Sparse Decomposition. There are one huge and some smaller  
301 short period signals associated to earthquakes, which are again detracted  
302 from the noise by Sparse Decomposition.

303 The trends detected by all methods look quite similar. In any case we  
304 obtain first a downdrift of 3.5 *kPa* over 2 years, followed by an updrift the  
305 same amount in the next seven years. As seen at the other data sets the  
306 boundary effects are very high at the Wavelet Decomposition.

### 307 3.5. Discussion

308 A summary of the observations described in the previous sections is given  
309 in table 2. The evaluation of the different decomposition methods was based  
310 on the following more or less qualitative criteria:

- 311 • How successful was the algorithm in decomposing the signal into a long  
312 and short period components?
- 313 • Did the algorithm find a short period event in the presence of back-  
314 ground noise?
- 315 • Does the algorithm create large effects at the boundaries of the time  
316 window?
- 317 • How much CPU time is needed for the decomposition?

318 From looking at table 2 one can conclude that none of the used methods  
319 for decomposition is perfect in every aspect. Harmonic and Wavelet are able  
320 to detect the short period features and perform also quite well in detracting  
321 the trend but their results, especially the results of Wavelet, show massive  
322 boundary effects. Because of this there is a high uncertainty if the shown  
323 decomposition is physically reasonable or not. On the other hand their com-  
324 puting efficiency is so high that the Harmonic and Wavelet Decomposition is  
325 nearly not restricted by the length of the given data.

326 The performance of EMD and EEMD is directly opposite to Harmonic  
327 and Wavelet. The EMD and EEMD perform very well on detracting the

Table 2: Overview of our results. ✓ indicates good, ● fair, and ✗ bad results.

			Harmonic	Wavelet	EMD	EEMD	Sparse
Decomposition	short period	SYN	✓	✓	✗	✗	✓
		MAR	●	●	✓	✗	✓
		CORK1	✓	✓	●	●	✓
		CORK2	✓	✓	✗	✗	✓
	long period	SYN	●	●	✓	●	✓
		MAR	✓	●	✓	✓	✓
		CORK1	✓	●	✓	✓	✓
		CORK2	●	●	✓	✓	✓
Boundary effects	SYN	✗	✗	✓	●	✓	
	MAR	●	✗	✓	✓	✓	
	CORK1	●	✗	✓	✓	✓	
	CORK2	●	✗	✓	✓	✓	
Computing efficiency			✓	✓	●	✗	✗

328 tides and show only small influences of boundary effects but their capability  
 329 of separating components with higher frequencies than the tides is restricted.  
 330 At least when the data is recorded with a sampling interval of 60 minutes.  
 331 Especially the EEMD fails because the added noise does not fade away in our  
 332 experiments. Overall we have seen in every data set that the large additional  
 333 computational effort of the EEMD compared to the EMD is not worthwhile  
 334 for the analysis of sea floor pressure data.

335 Very impressive is the capability of the Sparse Decomposition. It was able  
 336 to detract the short period components as well as the large period components  
 337 in every case. Contrary to the other methods, it was also able to detract the  
 338 noise from the meaningful short period components. A huge advantage is  
 339 also that the Sparse Decomposition does not have any boundary effects. Only  
 340 the computing efficiency needs to be improved.

## 341 4. Conclusion

342 To conclude our investigation we have to state that no method is perfect  
343 for every time series. For our data sets we got the best results by using the  
344 Sparse Decomposition. But at the moment it is not recommendable for time  
345 series with more than 200,000 measurements. For this kind of time series  
346 we recommend the EMD for long period contributions and the Harmonic  
347 Decomposition for the short ones. EEMD fails to improve the EMD in de-  
348 tecting and is not recommended due to its large computational needs. We  
349 obtained sometimes good results using the Wavelet Decomposition but they  
350 were never better than the results obtained by the Harmonic Decomposition,  
351 even in detecting earthquakes which is classically done by Wavelets.

352 It is obvious that the comparison of the computing efficiency is somewhat  
353 unfair as algorithms to calculate the FFT and Wavelet Transform are highly  
354 optimized whereas algorithms for EMD, EEMD and especially RFSS are  
355 not yet written for speed. However it is very likely that FFT and Wavelet  
356 Transform will always be faster however the difference to EMD, EEMD and  
357 RFSS will most likely shrink in the near future due to the improvement of  
358 the algorithms and maybe by developing parallel algorithms for them.

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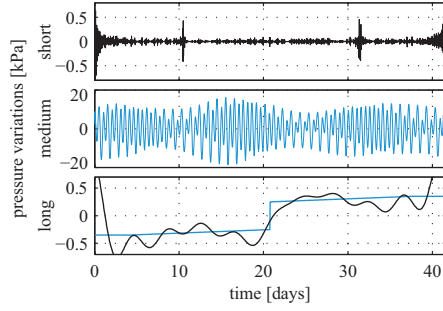
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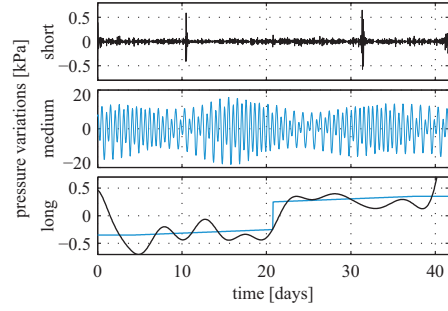


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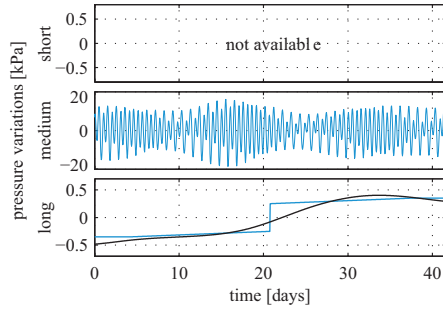
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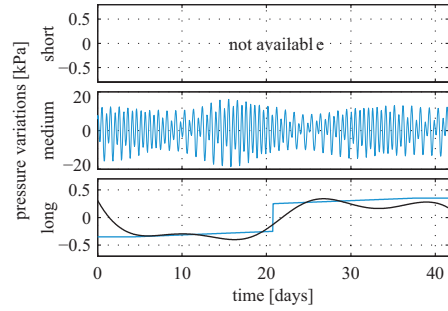
(a) Harmonic Decomposition



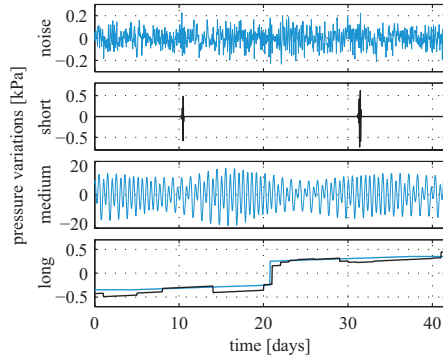
(b) Wavelet Decomposition



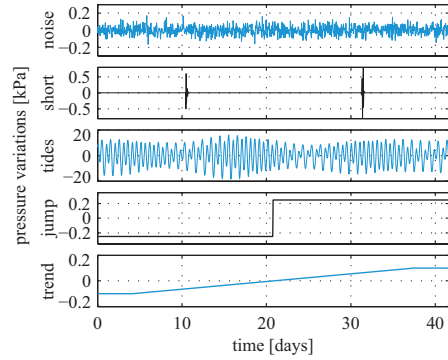
(c) EMD



(d) EEMD

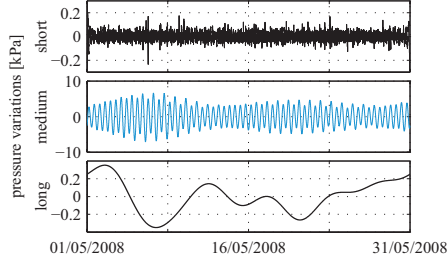


(e) Sparse Decomposition

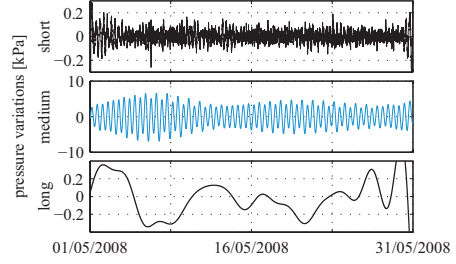


(f) synthetic data

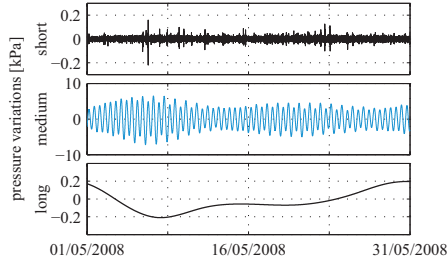
Figure 4: Decomposition of data set SYN. There are shown from the top to the bottom the short, medium and long time components. The real decomposition can be seen in figure 4(f). EMD and EEMD were not capable to detect features with a higher frequency than the tides.



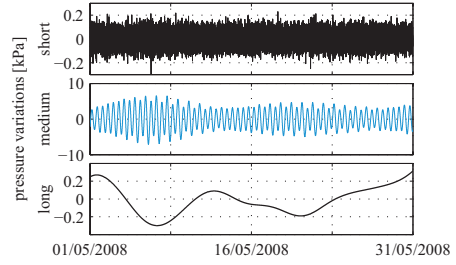
(a) Harmonic Decomposition



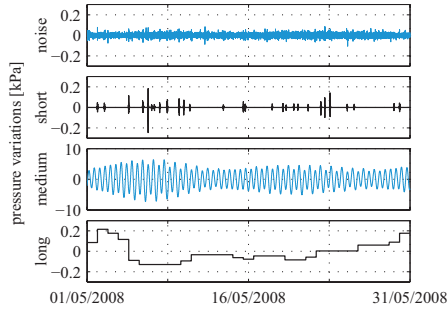
(b) Wavelet Decomposition



(c) EMD

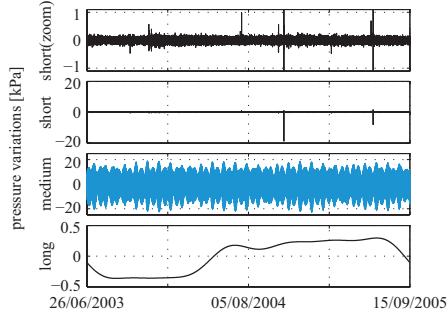


(d) EEMD

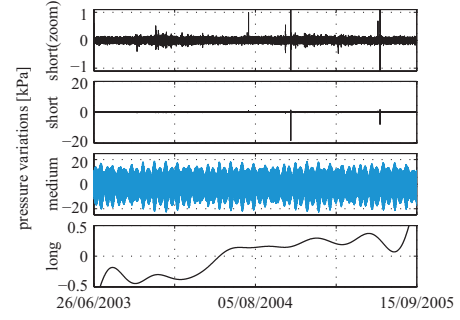


(e) Sparse Decomposition

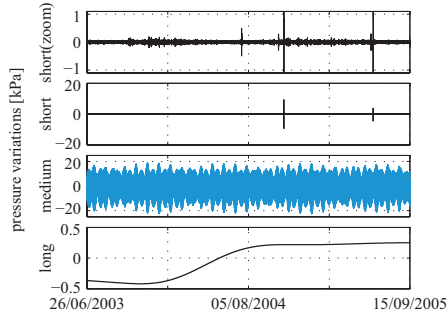
Figure 5: Decomposition of the data set MAR. There are shown from the top to the bottom the short, medium and long time components.



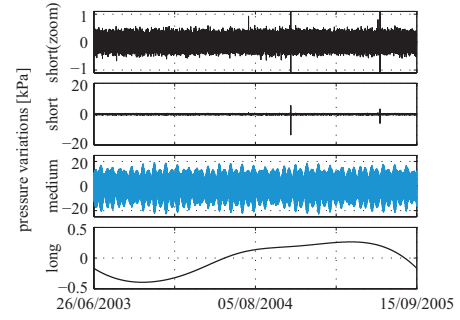
(a) Harmonic Decomposition



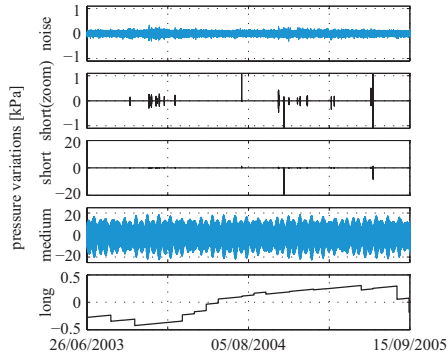
(b) Wavelet Decomposition



(c) EMD

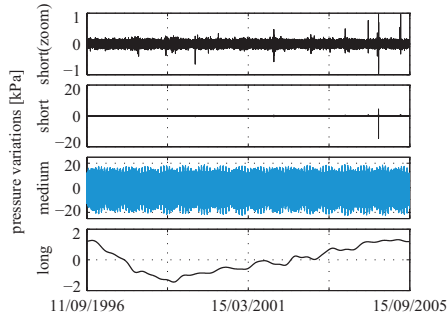


(d) EEMD

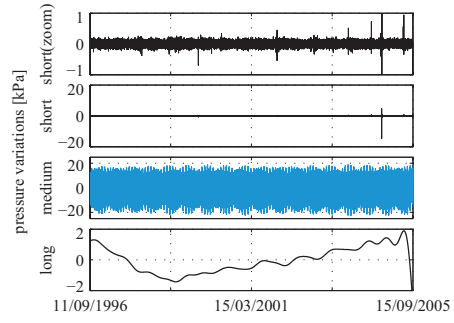


(e) Sparse Decomposition

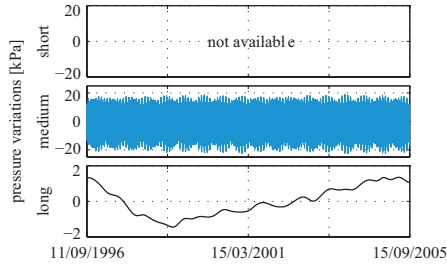
Figure 6: Decomposition of the data set CORK1. There are shown from the top to the bottom the short, medium and long time components.



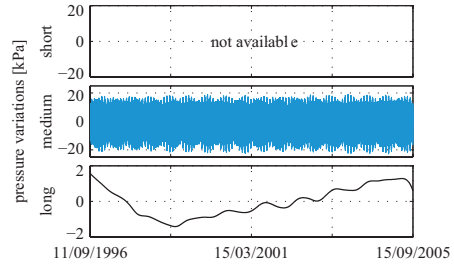
(a) Harmonic Decomposition



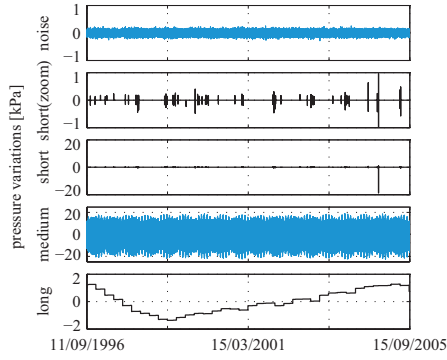
(b) Wavelet Decomposition



(c) EMD



(d) EEMD



(e) Sparse Decomposition

Figure 7: Decomposition of the data set CORK2. There are shown from the top to the bottom the short, medium and long time components. Since the short time components has features of different amplitudes these are also showed zoomed in. EMD and EEMD failed to detect the short period features.