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1 **STAlagmite dating by Radiocarbon (*star*): a software tool for reliable and fast age depth modelling**

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12

13 **Abstract**

14 Speleothems, secondary cave carbonates, are important tools for climate reconstruction, especially as  
15 they often can be very precisely dated with the U-Th method. If the U-Th method fails, dating becomes  
16 difficult, and often results in abandonment of samples and study sites. Radiocarbon dating is the only  
17 other radiometric dating technique applicable to the last ~50 ka, but presents complexities related to  
18 temporal variability of the reservoir effect in speleothems. Thus, radiocarbon dating of speleothems is  
19 not straightforward, and there are currently no publicly available tools to define proper age-depth  
20 relationships with this method.

21 Here, we present an improved version of a previously published radiocarbon based age-depth modelling  
22 approach (*star*, Lechleitner et al., 2016b), which is now made freely available. The software is easy to  
23 use and provides the possibility to obtain reliable age-depth relationships, without prior knowledge of  
24 reservoir effects and their variability. In addition, *star* is able to detect and handle growth stops and  
25 phases with different growth rates. We test *star* on artificially constructed data sets and illustrate steps  
26 to improve the model performance. Furthermore, we apply the new approach to published radiocarbon  
27 data of U-Th dated stalagmites. This offers the possibility to investigate the strengths and weaknesses of  
28 the new approach with respect to potentially significant long term trends in the radiocarbon reservoir  
29 effect, which might otherwise remain undetected. In summary, we have produced a valuable software,  
30 which easily enables to construct age-depth relationships on the basis of reservoir effect disturbed  
31 radiocarbon measurements.

32

33 **1. Introduction**

34 Stalagmites are well established archives for climate reconstruction of the Late Quaternary (e.g.,  
35 Fairchild and Baker, 2012). They offer the possibility to construct continuous, high resolution records of  
36 environmental variability. In combination with precise U-Th dating, important questions about the  
37 timing of climate-related events can be adequately addressed and leads and lags in the climate system  
38 can be investigated.

39 However, if the U-Th clock fails, either due to low U concentrations, especially challenging for young  
40 samples where not enough time passed for  $^{230}\text{Th}$  to build up, or due to a high detrital component  
41 embedded in the crystal lattice, stalagmites are stripped of their powerful strength. Apart from annual  
42 layer counting methods, applicable only on few specimens, the only alternative dating method is  
43 provided by radiocarbon. Moreover, the carbon isotope composition is believed not to be affected by  
44 diagenesis (Zhang et al., 2014), and thus radiocarbon dating can be a useful tool to date specimens  
45 where U-Th dating will fail due to open-system conditions related to diagenesis.

46 Radiocarbon dating of stalagmites and other secondary carbonates is complex and not straightforward,  
47 due to the *a priori* quantitatively unknown and temporally variable reservoir effect (dead carbon  
48 fraction, 'DCF'). The reservoir effect has been shown to vary on a wide range of time scales. On annual  
49 time scales variations of up to 10 percent modern carbon (pMC) in radiocarbon activity have been  
50 observed in cave drip water (Fohlmeister et al., 2010; Minami et al., 2015). Decadal to centennial scale  
51 variations have been reported to range around 10 pMC (Griffiths et al., 2012, Lechleitner et al., 2016)  
52 and on millennial time scales variations can be larger than 15 pMC (Oster et al., 2010; Noronha et al.,  
53 2014), with extreme values higher than 20 pMC observed (Bajo et al., 2017). Different carbon (C)  
54 sources and their relative contribution to stalagmite  $\text{CaCO}_3$  are responsible for these variations. The  
55 radiocarbon depleted host rock can introduce a reservoir effect of up to one radiocarbon half-life, but  
56 can also be negligible, depending on the conditions of carbonate dissolution. In addition, aged organic  
57 matter, either of the soil or from deep sources within the epikarst (e.g., Benavente et al., 2010; Noronha  
58 et al., 2015; Bergel et al., 2017) contributes to the reservoir effect. Variations in the reservoir effect are  
59 often related to changes in hydrology (Fohlmeister et al., 2010; Griffiths et al., 2012; Noronha et al.,  
60 2014; Lechleitner 2016; Bajo 2017) but can also be driven by aging or rejuvenation of organic matter  
61 sources or other, not yet understood processes (Oster et al., 2010; Rudzka et al., 2011).

62 First approaches to date stalagmites using radiocarbon corrected the measured radiocarbon age by an  
63 estimated and constant reservoir effect (e.g., Rudzka et al., 2012). A few years ago, Hua et al. (2012)  
64 proposed an interesting and powerful approach to date young speleothems. However, this method also  
65 still requires the assumption of a constant reservoir effect. Recently, Lechleitner et al. (2016b)  
66 developed a method with which radiocarbon dating of stalagmites is possible even without knowledge  
67 of the magnitude of the reservoir effect and without the need for the reservoir effect to remain  
68 constant in time. The only assumptions required in this approach are the stationarity of the reservoir  
69 effect (i.e., no long-term trends, but not necessarily constant) and no occurrence of major changes in  
70 the growth rate. This method has already been successfully applied to other stalagmite studies (Hua et  
71 al., 2017, Fohlmeister et al., 2017).

72 Here, we present an improved version of the approach published by Lechleitner et al. (2016b) now  
73 named *star*. Compared to the precursor work, the improved software version is now able to detect and  
74 handle growth stops as well as to find major changes in the growth rate. In addition, *star* advises the

75 user about the credibility of the dating approach by evaluating trends in speleothem proxies – especially  
76  $\delta^{13}\text{C}$  and Mg/Ca, which often relate to variations in the reservoir effect.

77

## 78 **2. Age modelling approach**

79 The basic principles behind the age-modelling approach are well described in Lechleitner et al., (2016b).  
80 In short, *star* uses the radioactive decay of radiocarbon to evaluate how much time has passed since  
81 deposition of the speleothem  $\text{CaCO}_3$ . The common decay equation

$$82 \quad A(t) = A(0) \cdot \exp(-\lambda t), \quad (1)$$

83 (with time,  $t$ , radiocarbon decay constant,  $\lambda$ , and the radiocarbon activity,  $A$ , where  $A(0)$  is not constant  
84 but a time-dependent function) can be translated to a depth scale,  $d$ , assuming a sufficiently constant  
85 growth rate, GR, by  $t = d/\text{GR}$ . Using the logarithm of equation (1) and replacing  $t$  by  $d$  and GR results in

$$86 \quad \ln(A(t)/A(0)) = -d \cdot \lambda / \text{GR}. \quad (2)$$

87 A linear fit is applied to the natural logarithm of the radiocarbon values over stalagmite depth. The  
88 slope,  $s$ , of this fit equals  $\lambda/\text{GR}$  and thus provides a direct estimate of the mean growth rate of the  
89 stalagmite. Using a point of known age, i.e., an anchor point, it is possible to deduce a first-estimate age-  
90 depth relationship. The anchor point might be the stalagmite top in case of an active drip feeding the  
91 stalagmite, or it might be the onset of the nuclear bomb peak if this atmospheric radiocarbon anomaly is  
92 found in the stalagmite. If a high quality U-Th date is available, this point can also be used as an anchor  
93 point.

94 So far this approach assumes that the initial radiocarbon activity in the speleothem remained constant  
95 through time. Being well aware that this is unlikely due to the changes in the atmospheric radiocarbon  
96 concentration (Reimer et al., 2013), an iterative process that accounts for atmospheric radiocarbon  
97 variation is used. Starting with the age control from the first-estimate age-depth model, the atmospheric  
98 radiocarbon values (using IntCal13; Reimer et al., 2013) at the estimated time of carbonate deposition  
99 can be used to correct for the variability of the initial radiocarbon concentration ( $A_0$ ) in the stalagmite.  
100 With the corrected radiocarbon activities, the fitting procedure is repeated, resulting in a more accurate  
101 mean growth rate and an improved age-depth estimate than in the prior iteration. In turn, the new age-  
102 depth model of the second iteration provides the possibility to perform a better correction of the initial  
103 radiocarbon activity by atmospheric radiocarbon values, which can then be used to further improve the  
104 age-depth relationship. The process is iteratively repeated until convergence of the mean growth rate is  
105 obtained, e.g., when growth rate is not changing by more than 1/1000 in successive iteration steps.

106 So far, this section described the already available approach. In the next section, the three new modules  
107 will be explained and discussed.

108

### 109 **2.1 First-order-check for stationarity of the radiocarbon reservoir effect**

110 Please note that it is not necessary to have any prior knowledge about the magnitude of the reservoir  
111 effect to apply this method and that the method even allows for a variable reservoir effect. However, an

112 important assumption for this method is the long-term stationarity of the reservoir effect (Lechleitner et  
113 al., 2016b), but this does not mean that the reservoir effect has to be constant through time. Cases  
114 where this assumption is violated will be discussed in sections 4.2 to 4.4.

115 The updated program version offers the possibility to evaluate the likelihood for the presence of long-  
116 term trends in the reservoir effect. This is done by analysing additional available stalagmite proxies, such  
117 as  $\delta^{13}\text{C}$  and Mg/Ca. Both proxies are known to be related to reservoir effect variations (e.g., Griffiths et  
118 al., 2012; Noronha et al., 2014; Lechleitner et al., 2016). If long-term trends are present in one or both of  
119 the additional datasets the likelihood for a long-term trend in the reservoir effect is relatively high and  
120 *star* will pause and notify the user about a potential non-stationarity of the reservoir effect. It is possible  
121 to resume the age-depth modelling after the pause, but the final modelling results should be critically  
122 scrutinised by the user.

123

## 124 **2.2 Detection and handling of growth stops**

125

126 While outlier detection for radiocarbon measurements influenced by variations in the reservoir effect  
127 are not very meaningful and thus not implemented, potential growth stops can be detected with a new  
128 function. Significant and fast transitions from low to high  $\text{In}(a_{14}\text{C})$  detected from old to young portions  
129 of the stalagmite are identified as potential growth stops. This method reliably detects growth stops for  
130 datasets with little variability in the reservoir effect, but is prone for false positive detections of growth  
131 stops if the reservoir effect is affected by large natural variability. It is therefore not possible to  
132 unequivocally define a growth stop, except with the help and experience of the user and taking into  
133 account other hints for growth stops, e.g., optically detectable layers in the stalagmite or anomalously  
134 large, rapid increases in Mg/Ca or  $\delta^{13}\text{C}$ . Therefore, *star* will only make suggestions on where growth  
135 stops might have occurred. The final decision has to be made by the user upon these suggestions.

136 After definition of the growth stop(s), the program checks which growth section the anchor point  
137 belongs to and starts with the age modelling of this section following the description in Sec. 2 (see also,  
138 Lechleitner et al., 2016b). For growth sections without an anchor point, the age-depth modelling  
139 procedure is slightly different. The average reservoir effect for the section with the anchor point is  
140 determined after modelling its age-depth relationship. With this average reservoir effect the  
141 radiocarbon measurements of the section(s) without an anchor point are corrected and calibrated. This  
142 ensemble of calibrated and reservoir effect corrected radiocarbon ages provides the most likely position  
143 of the mean growth rate determined by the slope of the depth vs  $\text{In}(a_{14}\text{C}(t))$  relationship. All errors for  
144 the calibration and the reservoir correction are rigorously handled. This method is then repeated for all  
145 growth sections without anchor point determined by the user.

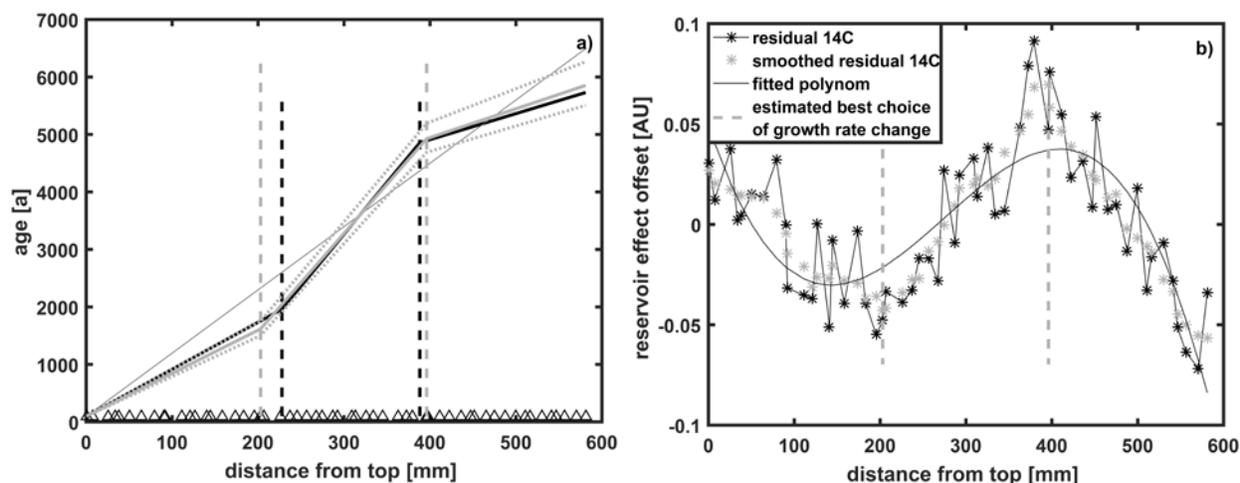
146 If an anchor point is available for each section bracketed by a growth stop, it is suggested to treat the  
147 sections as individual data sets. This is more precise as errors in sections without an anchor point are  
148 usually much larger due to the need for reservoir correction and calibration.

149

## 150 **2.3 Detection and handling of growth rate changes**

151 The most important improvement of the program is the newly implemented module for the detection  
 152 and handling of growth rate changes within the speleothem. For purposes of a better illustration we  
 153 produced an artificial radiocarbon data set for a 520 mm long stalagmite, with two major changes in  
 154 growth rate (Fig. 1a). The growth rate was prescribed to be 0.221 mm/a between 581 mm and ~388 mm  
 155 distance from top, 0.0554 mm/a between ~388 mm and 228 mm, and 0.1221 mm/a for the top part.  
 156 Prescribing that the top of the stalagmite was actively growing at the time of collection, the age  
 157 structure of this artificially constructed stalagmite is fixed, with growth starting ~5200 years before  
 158 today. Along the length of the hypothetical stalagmite 31 radiocarbon measurements were equally but  
 159 none-equidistantly distributed representing a possible straightforward sampling strategy for real  
 160 stalagmites. For the construction of the radiocarbon data set we accounted for the radiocarbon  
 161 concentration of the atmosphere and randomly added a reservoir effect of 15 +/- 3 % to the data, which  
 162 represent varying effects from the dilution of the atmospheric signal through radiocarbon devoid host  
 163 rock and pre-aged soil organic matter.

164



165  
 166 **Figure 1:** Artificial radiocarbon data set for a 520 mm long hypothetical stalagmite, with two major  
 167 changes in growth rate. a) Prescribed age-depth relationship in solid black, with position of radiocarbon  
 168 data points (open triangles). Dashed black lines represent the prescribed location of growth rate  
 169 changes. The modelled approximation of the age-depth relationship without taking into account growth  
 170 rate changes is represented by the thin grey line. The final result after identifying the depths where  
 171 growth rate changes occur is shown in thick grey, including error estimation (grey, dotted). Dashed grey  
 172 lines represent the modelled positions of growth rate change. b) Offsets from the average reservoir effect  
 173 (black stars) derived from the linear age-depth model are used to find the position of growth rate  
 174 changes (dashed grey lines). They are defined by the extreme values of the smoothed offset from the  
 175 average reservoir effect data series (grey stars). Solid thin polynomial reflects the best fit. The number of  
 176 the extreme values of the best-fit polynomial determines the number of growth rate changes detected by  
 177 the approach.

178

179 We use this artificial radiocarbon dataset to deduce the prescribed age-depth relationship with our  
 180 approach, trying to account for the changes in growth rate. First, the age-depth relationship is modelled

181 as if the growth rate would have been constant throughout the stalagmite growth (Fig 1a). While this is  
182 an appropriate approximation of the truth, this result would lead to systematic shifts in the reservoir  
183 effect (Fig. 1b), which can be calculated from the first-guess linear age-depth model. At depths where  
184 the modelled linear approach is older (younger) than the true age-depth relationship, the reservoir  
185 effect appears smaller (larger) than the average. Assuming that these second-order offsets are uniquely  
186 induced by age-offsets, this systematic can be used to define the locations of the growth rate change.  
187 The program is taught to recognise such typical structures. A structure with one maximum and one  
188 minimum is indicative for two occasions where the growth rate changed: one around the position of the  
189 maximum offset and one at the minimum offset (Fig. 1b). The strategy for defining the position of the  
190 growth rate changes is to smooth the reservoir effect variations (offset from the average) with a five-  
191 point running mean and to determine the extreme points of this smoothed data set. After testing, we  
192 found that this approach reliably finds the best estimate for the position(s) of a growth rate change.  
193 Afterwards, *star* individually evaluates the growth rate for each section between the depths with growth  
194 rate changes (Fig. 1a), starting with the section with the anchor point and using the same algorithm as  
195 described in Sec. 2.

196 This method is best suited to detect growth rate changes for alternating growth rates, e.g., from slow to  
197 faster growth and back to a slower growth. However, gradual changes cannot be reliably detected, e.g.,  
198 from fast to slow and even slower. In this scenario only one growth rate change is identified (fast to  
199 slow), in most cases close to the centre of the second growth rate section. This newly developed module  
200 allows to determine up to three positions of growth rate changes per growth section. Thus, for a  
201 stalagmite with one hiatus, up to six growth rate changes can be found and implemented in the age  
202 modelling procedure.

203

#### 204 2.4 Running the program

205 The program is written and tested in Matlab (versions R2016a and R2016b). The model comes with a  
206 short, one-page manual, in which the user is led through a short 'getting started' section by running a  
207 specific artificial dataset (from Lechleitner et al., 2016b). To become familiar with the program it is also  
208 possible to run a randomly generated data set and a real data set (Fohlmeister et al., 2017).

209 Crucial information for running the *star* are the radiocarbon measurements, which need to be provided  
210 in fraction Modern (fM) including errors and sample depths. In addition, an anchor point including its  
211 age uncertainty is necessary. After the user's evaluation of possible suggested growth stops an age-  
212 depth relationship for the stalagmite is provided. This result comes without any discussion of its  
213 reliability. If  $\delta^{13}\text{C}$  or Mg/Ca datasets (or both) were provided, *star* evaluates the reliability of the  
214 obtained age-depth relationship in terms of the state-of-the-art knowledge about the reservoir effect –  
215 proxy relationship (Griffiths et al., 2012, Noronha et al., 2014, Lechleitner et al., 2016b). As *star* is only  
216 evaluating long term trends for  $\delta^{13}\text{C}$  or Mg/Ca, the proxy data does not need to be provided in high  
217 resolution. This is especially useful in case only a limited amount of data is measured, e.g., in order to  
218 provide them for *star* to check the obtained age-depth relationship.

219 The number of radiocarbon data points does not need to be high to obtain good results, but the results  
220 will be better constrained with a higher number of radiocarbon measurements. Especially if the user is  
221 expecting a major change in growth rate we recommend to measure at least ten radiocarbon samples to

222 obtain a reliable result. Otherwise, it is prescribed to not test for changes, as our experience with this  
223 module showed that analysis of growth rate changes requires at least ten samples. Despite this, *star* can  
224 be run with only three available radiocarbon samples for simple age-depth models, but this is not  
225 advisable. The previous version of *star* was successfully used on a ~13cm long and 900 a old stalagmite  
226 with only six radiocarbon dates (Fohlmeister et al., 2017). In this example the radiocarbon reservoir  
227 effect was not varying strongly, and a reliable age model could be constructed with this approach.  
228 However, if the variation in the reservoir effect is large, it is advisable to measure a larger amount of  
229 samples. This reduces uncertainties in the fitting procedure and reduces the age error. The user can  
230 evaluate the extent of variation in the reservoir effect after obtaining the age-depth result for a first  
231 number of radiocarbon data points. If the age errors are large, then this is either due to a large variation  
232 in the reservoir effect or due a short growth period of the speleothem with respect to variations in the  
233 reservoir effect. *Star* can provide good results for stalagmites that grew over sufficiently long time  
234 periods ( $\sim > 2000$  a), when the relative magnitude of variations in the reservoir effect becomes less  
235 important. For stalagmites with shorter growth periods ( $\sim < 1000$  a) reservoir effect variations can  
236 significantly affect the reliability of the constructed age model.

237

### 238 **3. Limits of the new functions**

239

#### 240 **3.1 Stationarity of reservoir effects**

241 As discussed in many studies investigating the influence of hydrology on the radiocarbon reservoir effect  
242 (DCF), there is a relationship between DCF and other hydrology related proxies such as Mg/Ca or  $\delta^{13}\text{C}$   
243 (Griffiths et al., 2012; Lechleitner et al., 2016a; Bajo et al., 2017). Usually this relationship is argued to be  
244 established by the negative correlation between the amount of precipitation and the Mg/Ca ratio  
245 caused by incongruent carbonate dissolution and prior calcite precipitation (e.g., Fairchild and Treble,  
246 2009; Sinclair et al., 2012). The stable C isotope composition is influenced by variations in drip rate  
247 (infiltration of meteoric water and karst hydrology) through prior calcite precipitation and fractionation  
248 effects on the top of the stalagmite (e.g., Dreybrodt, 2008; Scholz et al., 2009; Dreybrodt and Scholz,  
249 2011; Deininger et al., 2012; Fohlmeister et al., 2018). In contrast, the amount of precipitation is often  
250 correlated with the DCF as a result of variations of the carbonate dissolution conditions (Fohlmeister et  
251 al., 2010; 2011; Griffiths et al., 2012). Based on those assumptions, *star* checks for long-term trends in  
252 Mg/Ca and  $\delta^{13}\text{C}$  to predict possible trends in the reservoir effect.

253 Studies where reservoir effect and Mg/Ca or  $\delta^{13}\text{C}$  showed contemporaneous long-term trends are  
254 available (Scholz et al., 2012; Bajo et al, 2017) and support our method of DCF trend detection.  
255 However, the knowledge on C-transfer dynamics in karst systems is still limited (Lechleitner et al.,  
256 2016b) and the hydrology-based relationship between the reservoir effect and the other proxies might  
257 be violated if other processes counteract the known mechanisms. Therefore, predicting trends in the  
258 reservoir effect with the use of ancillary proxies should still be treated with great care, and the results  
259 should in any case be evaluated by the user. Future improvements in the understanding of C-transfer  
260 dynamics from the soil to the cave system will allow for a more reliable prediction of reservoir effect  
261 trends.

262

263 **3.2 Detection of growth rate changes**

264 We produced three sets of 20000 synthetic age-depth models each to analyse how variations in the  
 265 reservoir effect, growth rate, and the number of radiocarbon measurements affect the detection and  
 266 position of growth rate changes, as well as the precision of the modelled age-depth relationships. The  
 267 three sets differ in their prescribed growth rate ranges (10 to 100  $\mu\text{m/a}$  and 50 to 500  $\mu\text{m/a}$ ) and in the  
 268 DCF variability (between 12 to 17% and between 6 and 23 %; Tab. 1). The artificially constructed growth  
 269 history and accordingly prescribed synthetic radiocarbon data were produced completely randomly  
 270 (uniform distribution) but within given constraints. Each synthetic stalagmite was prescribed to be  
 271 between 10 and 20 cm long and had between 10 and 40 radiocarbon measurements, which were evenly  
 272 but not equidistantly distributed across the length of the synthetic dataset. The depth of the growth rate  
 273 change was randomly prescribed to be somewhere within the second third of the stalagmite. The  
 274 growth rates of the two sections were determined randomly and independently from each other; i.e.,  
 275 the growth rate differences can be large or small. Each stalagmite stopped growing recently, i.e., the  
 276 anchor point for all realizations is present-day at the stalagmite top.

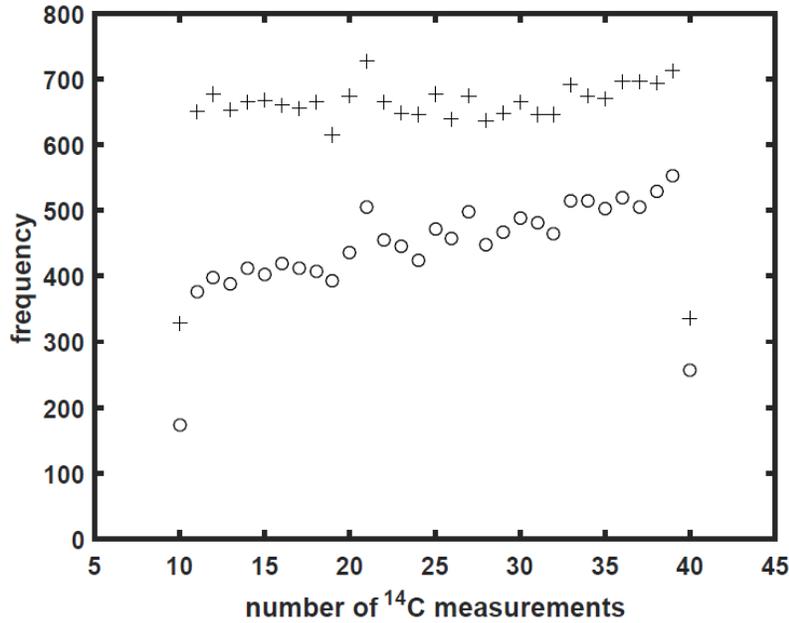
277

278 **Tab. 1:** Parameters and prescribed ranges for each of the three experiments. The ‘normal’ experiment  
 279 accounts for small variations in growth rate and DCF, while the ‘high DCF’ experiment has a large  
 280 variation in the reservoir effect and the ‘fast growth’ experiment is designed to investigate our model  
 281 approach under faster growth rates. For each experiment 20000 artificial data were generated.

| Experi-<br>ment | Length<br>range<br>[cm] | Number<br>of 14C<br>points | Location of<br>growth rate<br>change | Growth<br>rate<br>range<br>[ $\mu\text{m/a}$ ] | DCF<br>variability<br>[%] | Growth<br>rate<br>change<br>detected<br>[%] | Median relative<br>offset in timing of<br>growth rate change<br>[%] |
|-----------------|-------------------------|----------------------------|--------------------------------------|--|---------------------------|---|---|
| normal          | 10-20                   | 10-40                      | middle third                         | 10-100   | 12-17                     | 66.3  | 10.5  |
| high<br>DCF     | 10-20                   | 10-40                      | middle third                         | 10-100   | 6-23                      | 34.9  | 19.9  |
| fast<br>growth  | 10-20                   | 10-40                      | middle third                         | 50-500   | 12-17                     | 29.1  | 17.2  |

282

283 The detection rate of growth rate changes increases with more radiocarbon measurements (Fig. 2). This  
 284 is valid for all three experiments, but at different levels. While for the ‘normal’ experiment about 2/3 of  
 285 the realizations detected a growth rate change, the success rate of the other two experiments is only  
 286 about 1/3 (compare Tab. 1). The success rate of the detection for the ‘high DCF’ experiment is lower as a  
 287 result of the large reservoir effect variability, which is responsible for significant noise on the  
 288 radiocarbon decay trend that masks any growth rate changes. This is especially true for stalagmites  
 289 covering only a short period of time.



290

291 **Fig. 2:** Frequency of randomly determined number of radiocarbon measurements (crosses) is evenly  
 292 distributed for the 'normal' experiment. The open circles represent the number of artificially produced  
 293 data sets with detected growth rate changes for the same experiment. Note the increase in detected  
 294 growth rate changes with increasing number of radiocarbon measurements per sample.

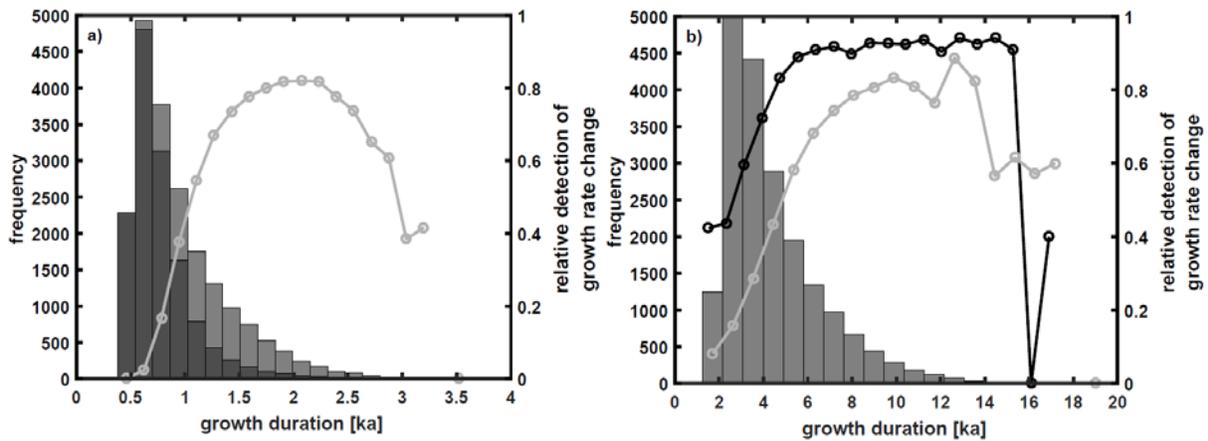
295

296 The reason for the low detection rate in the 'fast growth' experiment is related to the short time period  
 297 covered by the artificially constructed stalagmite data sets. Short growth periods do not allow for  
 298 enough radiocarbon decay to occur for a good fit. Although the reservoir effect variations are also kept  
 299 small for this experiment, the signal (radiocarbon decay) to noise (reservoir effect variations) ratio  
 300 remains too high to enable our approach to detect growth rate changes. This effect is well visible when  
 301 comparing the relative detection rate over the growth duration of the stalagmite (Fig. 3). For stalagmites  
 302 covering only 500 years the detection rate of a growth rate change is very low, but increases rapidly  
 303 when stalagmites grow over longer time periods. For stalagmites growing over a period of more than  
 304 1500 years the detection rate reaches ~80% for the 'fast growth' experiment. For the 'normal' and 'high  
 305 DCF' experiments the detection rate also strongly increases with growth duration (Fig. 3).

306

307

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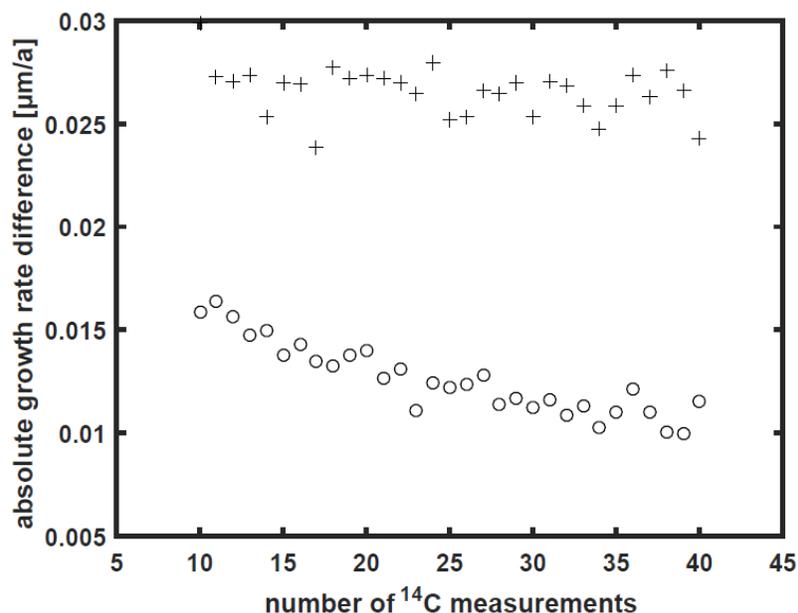
310 **Fig. 3:** Frequency distribution and the relative detection of growth rate changes over the growth period  
 311 length of the artificially constructed stalagmite age-depth models. a) Frequency distribution for all  
 312 realisations of the 'fast growth' experiment (light grey bars) are shown as well as for those realisations  
 313 with no detection (dark grey bars). Grey circles show the detection rate of growth rate changes. b)  
 314 Frequency distribution for all realizations of the 'normal' experiment (for the 'high DCF' experiment the  
 315 distribution looks similar) and its relative detection rate of the growth rate change (black circles). Grey  
 316 circles represent the detection rate for the 'high DCF' experiment.

317

318 The detection rate of growth rate changes varies strongly and appears to decrease for longer data sets  
 319 (> 2.5 ka for the 'fast growth' experiment, >13 ka for both other experiments). However, this is an  
 320 artefact due to the low number of long growing synthetic datasets constructed here, as the detection  
 321 rate for data sets with a long growth period should remain high. This is indicated by the low relative  
 322 proportion of growth rate change detection for long growing stalagmites of the 'fast growth' experiment  
 323 (Fig. 3; growth period between present day and 2.5 to ~3.6 ka) and the high detection rate for the  
 324 'normal' experiment for the same growth period.

325 Interestingly, the relative detection rate for all three experiments is not the same for similar growth  
 326 durations. For the 'high DCF' experiment this is not a surprise due to the strong noise introduced by the  
 327 large reservoir effect variability. It is somewhat surprising however for the experiments which only differ  
 328 by their growth rates. For example, the detection rate of a growth rate change for a typical 2 ka old  
 329 stalagmite within the 'fast growth' data set is about 80% while for the 'normal' experiment a successful  
 330 detection is only obtained for only about 40% of all synthetic data sets. This difference is caused by the  
 331 different absolute change in growth rate changes possible for each data set, as the program more easily  
 332 detects larger absolute variations in growth rate. For the 'normal' experiments the growth rate was  
 333 prescribed to be within a range of 10 to 100  $\mu\text{m}$ , and thus the absolute growth rate change is much  
 334 smaller (i.e., maximum 90  $\mu\text{m}$ ) than what is possible for a 'fast growth' stalagmite, where the growth  
 335 range was prescribed between 50 to 500  $\mu\text{m}$  (maximum change 450  $\mu\text{m}$ ). Larger absolute variations in  
 336 growth rate can be much more easily detected by our program. This can be also expressed in a different  
 337 way: the longer the period where speleothems grow with the same growth rate, the more likely it is to  
 338 detect also small absolute changes in growth rate. With more radiocarbon measurements available it  
 339 becomes easier to detect smaller absolute growth rate changes as well (Fig. 4). A similar behaviour is  
 340 detected for all three types of experiment.

341



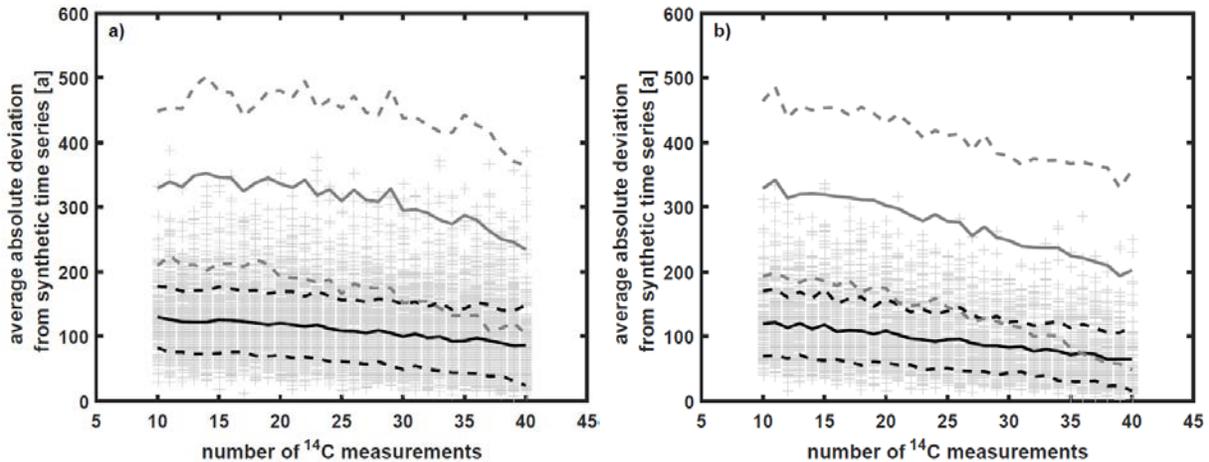
342

343 **Fig. 4:** The average for the absolute difference of growth rates for the successful detection of growth rate  
344 changes for the realizations of the 'normal' experiment is  $\sim 0.026 \mu\text{m/a}$  (crosses) for any number of  
345 radiocarbon measurements. The absolute difference of growth rates with an unsuccessful detection of  
346 growth rate changes decreases with the number of radiocarbon measurements (circles).

347

348 An additional positive effect of a larger number of radiocarbon measurements for a given (synthetically  
349 produced) stalagmite data set is the smaller average absolute age deviation between the modelled and  
350 artificially produced age-depth relationships (Fig. 5). For the 'normal' experiment the average absolute  
351 age deviation for realizations with successful growth rate change detection is reduced from  $\sim 120$  to  
352  $\sim 100$  a when the number of radiocarbon measurements is increased from 10 to 40. If the growth rate  
353 change was not detected, the average deviation between the modelled and artificially produced age-  
354 depth relationships is even smaller. In this case, the average absolute age offset is reduced from about  
355 110 a (with 10 samples) to  $\sim 80$  a (with 40 samples; Fig. 5). This proves very nicely that for those cases  
356 where the growth rate change has not been detected (e.g., due to low absolute growth rate differences  
357 or short growth duration), the average absolute age offset between modelled and true age-depth  
358 relationship is already relatively small. In other words, in cases where the average absolute growth  
359 offset for the modelled linear age-depth relationship is large, a growth rate change is usually detected.  
360 Then the recalculation of the age model with two phases of different growth rates minimises the age  
361 offset. This shows that even if growth rate changes are not detected, the obtained age-depth  
362 relationship is reliable.

363



364

365 **Fig. 5:** Absolute value of the average age offset between age-depth modelling results and their actual  
 366 synthetic age-depth relationship for the 'normal' experiment (Tab. 1). a) Results for cases where the  
 367 growth rate change was detected; b) results for cases where the growth rate change detection failed.  
 368 Crosses represent the results of individual realizations, while solid and dashed black lines represent the  
 369 average and standard deviation of the individual realizations for a given number of radiocarbon  
 370 measurements. Grey solid and dashed lines represent the average absolute age offset and standard  
 371 deviation when the range in DCF is between 23 and 6% ('high DCF' experiment, Tab. 1). Individual results  
 372 for this scenario are not shown.

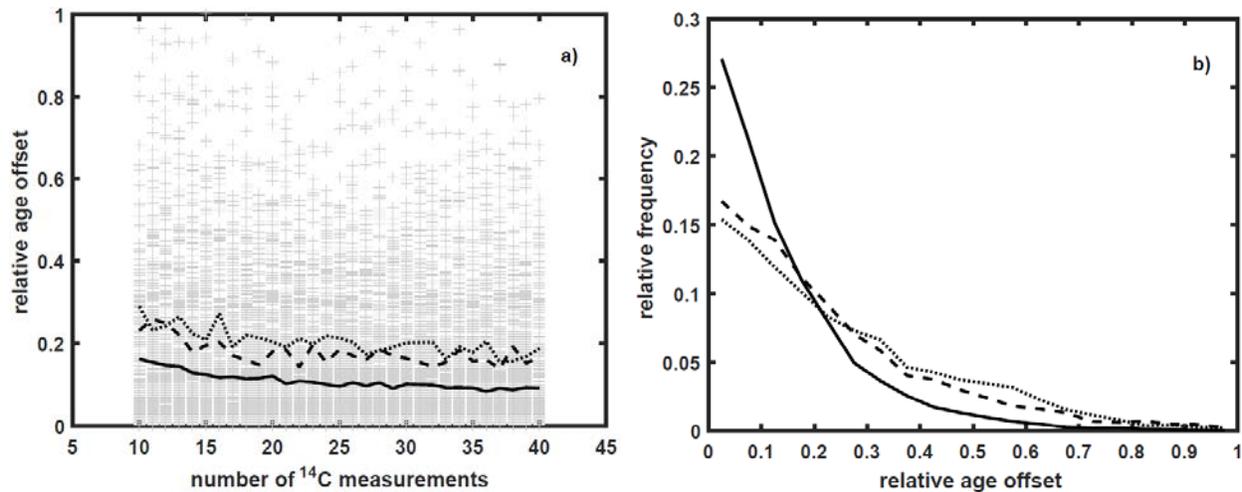
373

374 The age offset between modelled and artificially constructed age-depth relationship becomes much  
 375 larger if the radiocarbon reservoir effect strongly varies (Fig. 5). For the successful detection of a growth  
 376 rate change in the 'high DCF' experiment the average age offset between modelled and true age-depth  
 377 relationship is reduced from ~350 to 250 a when the number of radiocarbon measurements is increased  
 378 from 10 to 40. If the growth rate change is not detected, the age offset is reduced from ~330 to 200 a  
 379 with increasing number of radiocarbon measurements. Again, the age offset for the unsuccessful  
 380 detection of growth rate changes is smaller than for the successful growth rate change detections.

381 This large average age offset between modelled and true age-depth relationship for the 'high DCF'  
 382 experiments should not concern potential users. A data compilation of available reservoir effect  
 383 variations of published records indicates that usually the reservoir effect variations are in the range of  
 384 +/- 2.5 % (Hua et al., 2017), similar as prescribed for the 'normal' experiment in this study. The large DCF  
 385 variation of the 'high DCF' experiment (+/- 8.5 %) are only chosen to better exemplify the influence of  
 386 the strength of reservoir effect variations and were only observed in extreme locations so far (e.g.,  
 387 Genty et al., 2001; Bajo et al., 2017).

388 Our method reliably reproduces the timing of growth rate changes in synthetically produced stalagmite  
 389 datasets (Fig. 6a). For all synthetic datasets produced, the relative age offset between prescribed and  
 390 modelled timing of the growth rate change is very small and nearly independent of the amount of  
 391 radiocarbon measurements for more than ~20 measurements.

392



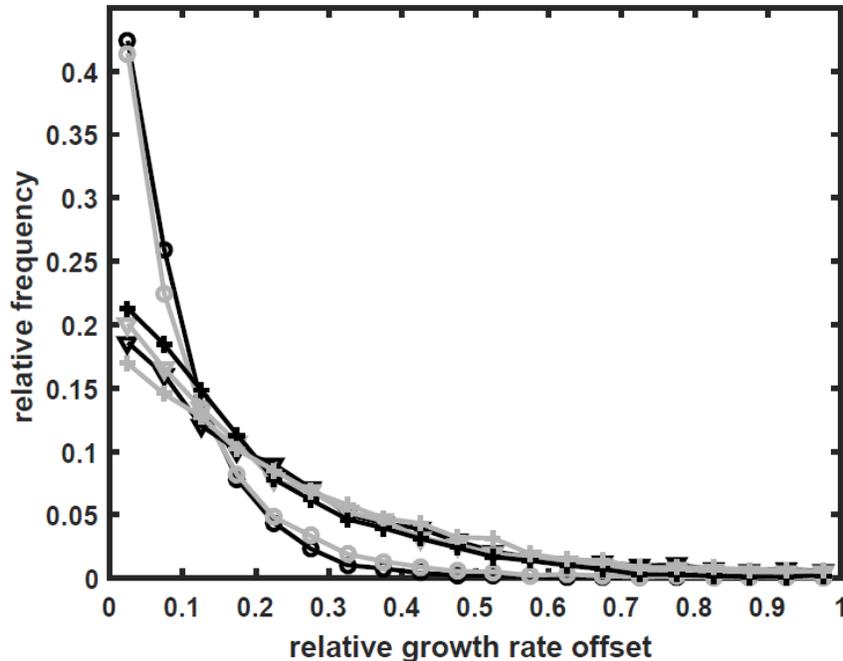
393

394 *Fig. 6: a) The relative age offset of the modelled vs prescribed timing of the growth rate changes over the*  
 395 *number of radiocarbon measurements. Grey crosses represent the individual offset of the modelled vs*  
 396 *prescribed timing of the growth rate change for the 'normal' experiment. The solid line indicates the*  
 397 *median offset for a given amount of radiocarbon measurements in this experiment. The median values*  
 398 *for the 'high DCF' and 'fast growth' experiment are represented by the dotted and dashed lines. b)*  
 399 *Relative frequency of the relative age offsets for the timing of the growth rate change. Line coding is as*  
 400 *in a).*

401

402 For the 'normal' experiment, the median relative age offset for the timing of the growth rate change is  
 403 ~10.5 %. The offset is slightly larger for the 'high DCF' (19.9 %) and the 'fast growth' (17.2 %)  
 404 experiments, but again not strongly affected by the number of measurements, especially when >20  
 405 samples are available. Approximately 75 % of all successfully detected growth rate changes find the  
 406 position within a 20 % range for the 'normal' experiment. Only about 0.3 % of all successfully detected  
 407 growth rate changes have an offset for the timing of the age offset of larger than 100 %.

408 Similar observations can be drawn when comparing the prescribed and modelled growth rates before  
 409 and after the timing of growth rate change (Fig. 7). Both growth rates, before and after the growth rate  
 410 change are well reproduced by star, in most cases with only a small offset. About 90 % (85%) of all  
 411 iterations have a relative growth rate offset not larger than 20 % for growth rate before (after) the  
 412 change in the 'normal' experiment. The relative growth rate offsets for the other two experiments are  
 413 larger. More than 55 % of all iterations for both other experiments obtain offsets smaller than 20 % for  
 414 growth rates before and after the growth rate change.



415

416 *Fig. 7: Relative growth rate offsets for all three types of experiments for the period before (grey) and*  
 417 *after (black) the growth rate change. Circles – ‘normal’, plus signs – ‘fast growth’ and triangles – ‘high*  
 418 *DCF’ experiment.*

419

420

#### 421 **4. Application to existing speleothem 14C data**

422 The application of our method to ‘real’ stalagmites is still difficult, due to the paucity of published  
 423 datasets that provide a precise U-Th based chronology and radiocarbon measurements spanning longer  
 424 than ~ 500 years. Here, we focus on four stalagmites, starting with a specimen that fulfils all  
 425 requirements for the use of our age-depth modelling approach (Sec. 4.1). It is easier to learn about the  
 426 limits of this approach with examples where the age-depth modelling is not entirely successful, thus we  
 427 successively choose specimen with an increased degree of complexity: (1) trends in  $\delta^{13}\text{C}$  or Mg/Ca which  
 428 hint to a violation of the stationarity assumption in the reservoir effect (Sec. 4.2) and (2) multiple  
 429 changes in growth rate (Sec. 4.3). Finally, we apply the method even to a stalagmite with secondary  
 430 long-term reservoir effect variations, which can be approximated by a polynomial of fourth order  
 431 (Sec.4.4). This approach illustrates the effects of trends in the reservoir effect on the calculation of age-  
 432 depth models.

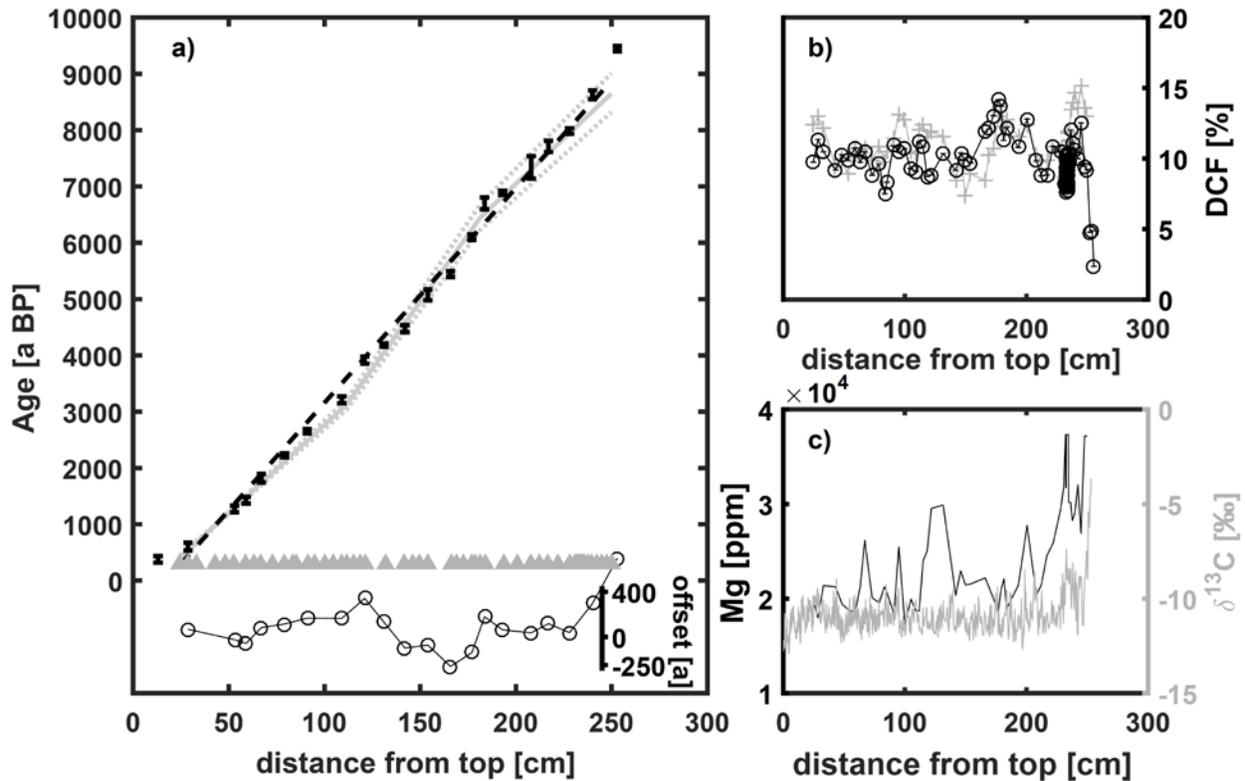
433

#### 434 **4.1 Stalagmite HS4 – Heshang cave**

435 As in Lechleitner et al. (2016b), we first focus on the precisely U-Th dated stalagmite HS4 from Heshang  
 436 Cave, China, which grew during the Holocene and has more than 80 radiocarbon measurements  
 437 (Noronha et al., 2014). We compare the original age-depth model (Hu et al., 2008) with the age-depth

438 relationship published with the first version of *star* (Lechleitner et al., 2016) and with the model output  
 439 for the recent version of our approach (Fig. 8a). In addition, we show the DCF as derived for the U-Th  
 440 based age-depth model and the results for the recent approach (Fig. 8b) as well as Mg/Ca and  $\delta^{13}\text{C}$   
 441 values (Fig. 8c; Noronha et al., 2014, Hu et al., 2008).

442



443

444 **Fig. 8:** a) Comparison of age-depth relationships as provided by U-Th dating (black signs, with error bars)  
 445 and from radiocarbon measurements using the first version of *star* (dashed black line; Lechleitner et al.,  
 446 2016) and the version presented in this study (solid grey line, plus error envelope – dotted grey lines). The  
 447 anchor point for both versions was a U-Th age of 0.985 ka at 43 cm depth from top. Triangles represent  
 448 the depths of radiocarbon measurements. Open circles show the deviation between the U-Th ages and  
 449 result of the present *star*-version. b) DCF as calculated based on the U-Th chronology in Noronha et al.  
 450 (2014, black) and as resulted from the radiocarbon age-depth modelling (this study, grey). c) The Mg/Ca  
 451 and  $\delta^{13}\text{C}$  data sets show no long-term trend, corroborating the absence of secular trends in DCF.

452

453 The ancillary  $\delta^{13}\text{C}$  values are not affected by consistent and long-term trends, while Mg/Ca only shows a  
 454 weak linear trend within the oldest fifth of the record (Fig. 8c). Thus, a warning is given by *star* that the  
 455 stationarity of the reservoir effect might be compromised. However, in this case, the high precision U-Th  
 456 chronology allows calculation of the true reservoir effect (Noronha et al. 2014), which indeed proves to  
 457 be stationary but with a noisy structure (Fig. 8b). This allows us to apply our approach and highlights the  
 458 fact that even if there are trends in the ancillary proxies, this does not necessarily translate to non-  
 459 stationarity in the reservoir effect, as these relationships are not perfect. Thus, a trends in the ancillary

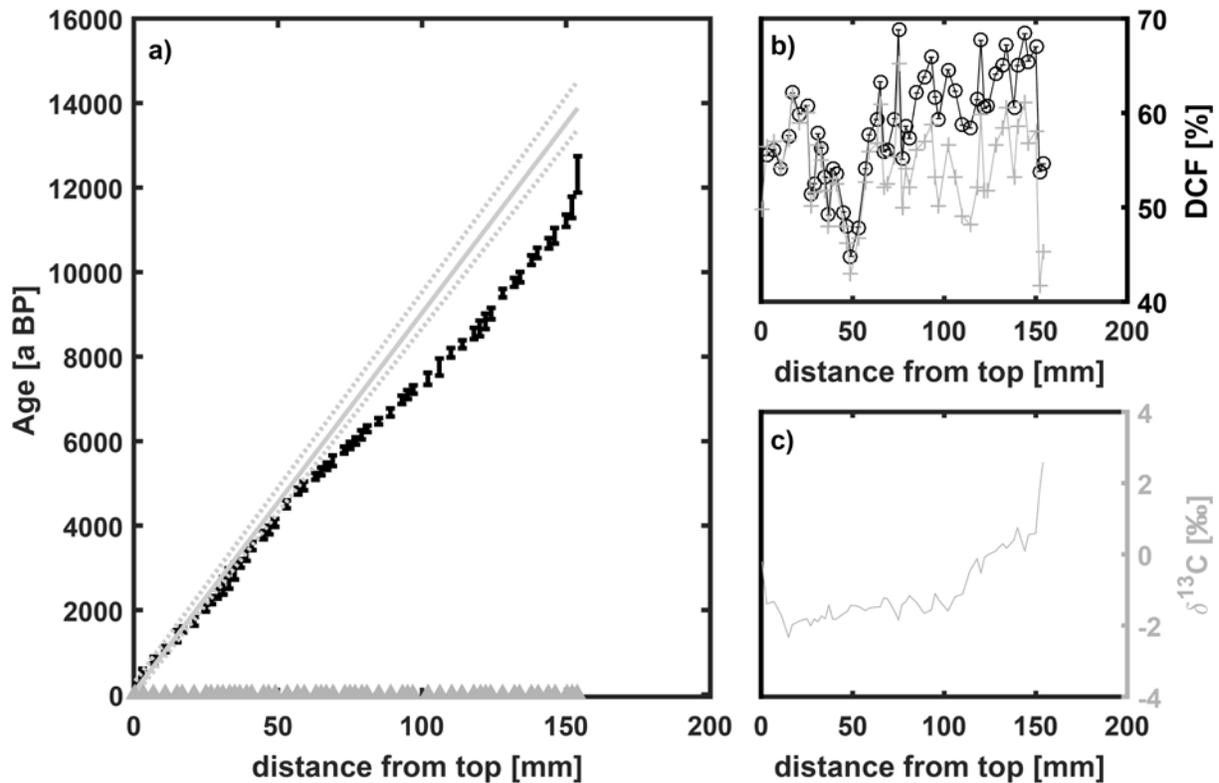
460 proxies does not preclude the use of *star*, but rather the user needs to assess the likelihood of a  
461 relationship between ancillary proxies and DCF. The DCF varies between ~7 and 14 % (+/-3.5 % around  
462 the mean value) and thus is comparable with the 'normal' dataset of synthetic records, discussed in Sec.  
463 3.2. With its long growth duration (~9 ka) and fast growth rate (average 270µm/a), this specimen is  
464 perfectly suited to apply *star*. Indeed, the model results compare well to the U-Th ages, especially when  
465 applying the updated model version presented here, as the true growth history is reproduced much  
466 more closely than in the previous model version (Fig. 8a). This is a result of the newly included function  
467 to detect and implement growth rate changes. The excellent match between calculated and modelled  
468 DCF values emphasizes how well *star* can capture the real growth history of a stalagmite (Fig. 8b).

469

#### 470 **4.2 Stalagmite CC26 - Corchia cave**

471 A recently published dataset from stalagmite CC26 from Corchia Cave, Italy, includes a precise U-Th  
472 based chronology as well as Mg/Ca,  $\delta^{13}\text{C}$ , and radiocarbon data (Regattieri et al., 2014; Bajo et al., 2017).  
473 While no long term trend in Mg/Ca is detected,  $\delta^{13}\text{C}$  values gradually decrease from +3 to -2‰ (Fig 9c).  
474 It is also worth noting that the  $\delta^{13}\text{C}$  values in this stalagmite are exceptionally high compared to other  
475 stalagmites, an indication of the unusual depositional conditions in this cave (Bajo et al., 2017). The  
476 trend in  $\delta^{13}\text{C}$  prompts a warning about possibly compromised age-depth modelling in the software. This  
477 is indeed the case, as the U-Th-derived DCF is affected by a long-term trend, synchronous with the  $\delta^{13}\text{C}$   
478 trend (Fig. 9b; Bajo et al., 2017). This threatens the stationarity assumption of our approach. Here, we  
479 investigate the impact of this trend in DCF on the resulting radiocarbon based chronology (Fig. 9a).

480



482

483 **Fig. 9:** a) True, U-Th based age depth model of stalagmite CC26 (black, Bajo et al. 2017) and the result of  
 484 the radiocarbon based age-depth model (grey) with uncertainties (grey shaded area). The anchor point is  
 485 102 years at 0.5 mm from top. Black signs represent U-Th dates with their errors. Grey triangles at the  
 486 bottom indicate the depths of radiocarbon measurements. b) Reservoir effect variations over depth with  
 487 respect to the U-Th based age depth model (black) and after the radiocarbon based one (grey). c) Carbon  
 488 isotope composition over depth of stalagmite CC26.

489

490 The modelled age-depth relationship follows the U-Th based chronology faithfully in the youngest part  
 491 of the record (~ 6 ka to present, Fig. 9a). However, the two age models increasingly diverge in the earlier  
 492 part of the record, as the true DCF steadily increases and moves away from stationarity (Fig. 9b). The  
 493 radiocarbon based age-depth modelling approach is not able to detect the growth rate change at ~60-70  
 494 cm depth. As a result, *star* interprets the DCF trend as a considerably older growth history (~1500 a  
 495 older at the bottom; Fig. 9a). This example illustrates well how providing additional ancillary proxies that  
 496 reflect processes affecting the DCF can be crucial for the final evaluation of the age-depth model. On a  
 497 positive note, we show that the model agrees very well with the U-Th chronology for the younger part  
 498 of CC26, where the stationarity criterion is met, and that the very high and variable DCF (between 44  
 499 and 64 %) does not preclude a successful application of this approach.

500 In addition, we tested how the input of less radiocarbon data affects the age-depth modelling result.  
 501 The final result is nearly unchanged even removing one third or half of the radiocarbon measurements.  
 502 The influence of a few, single measurement points was also tested by removing them individually. As

503 expected, the final result of the age-depth model does not change if the values we tested lie in the  
504 centre of the stalagmite. However, if radiocarbon measurements are removed at the stalagmite top, the  
505 model result changes substantially, as *star* finds two points where growth rate changes could have  
506 occurred. Interestingly, under this conditions the model performs slightly better for the older part (>6  
507 ka) than the youngest interval. Thus the top and bottom of a target stalagmite require denser sampling,  
508 while within the stalagmite sampling density does not be as high. This is useful especially with respect to  
509 the considerable cost of radiocarbon measurements.

510

#### 511 **4.3 Stalagmite MC3, Moaning Cave**

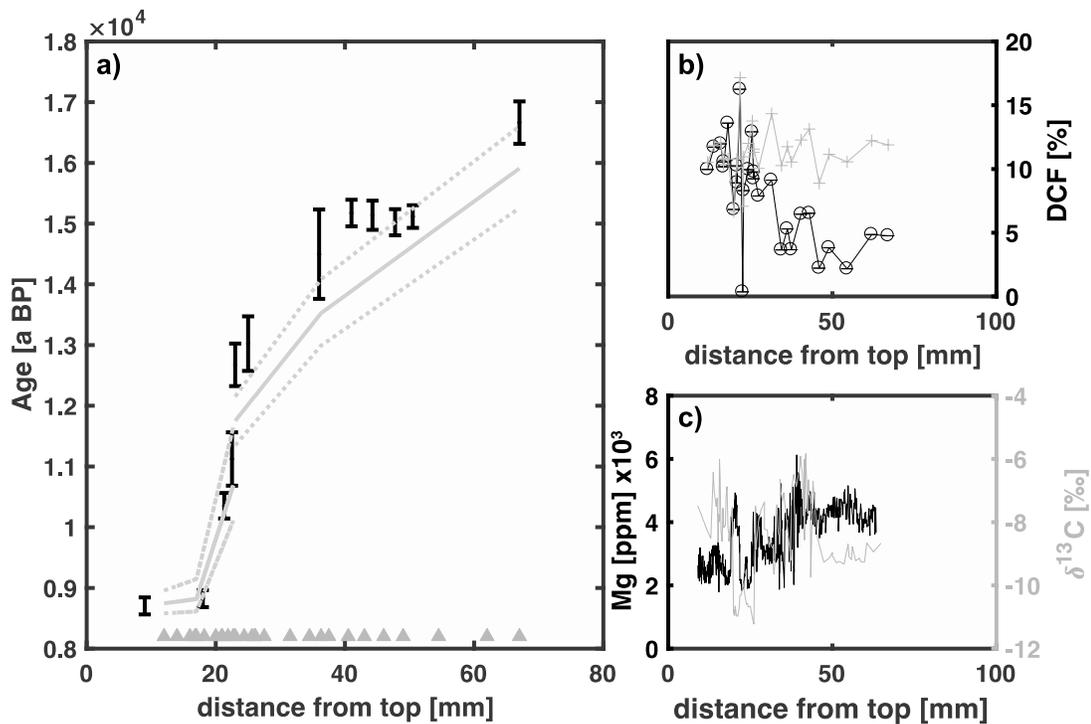
512 Next, we apply our model to flowstone MC3 from Moaning cave, Nevada (Oster et al., 2010), where the  
513 anchor point is located in the flowstone section with a long-term trend in DCF (derived from the U-Th  
514 chronology; Fig. 10b). Previous studies have highlighted the complicated influences on  $\delta^{13}\text{C}$  and Mg/Ca  
515 in this cave system, which are believed to reflect not only humidity changes but also shifts in the drip  
516 centre of the flowstone (Oster et al., 2009). While  $\delta^{13}\text{C}$  data in stalagmite CC26 from Corchia cave  
517 reflected the presence of a trend in DCF, the stable isotope data available for MC3 does not show any  
518 long-term trend but large fluctuations (Fig. 10c). In contrast, Mg shows a long term trend (Fig. 10c),  
519 which illustrates the advantage of having both proxies available.

520 MC3 has 12 U-Th dated depths that reveal its complicated growth history. Three phases with different  
521 growth rates can be derived. A fast growth on the top (between ~10 and 20 mm), slow growth between  
522 ~20 and 25 mm culminating in extremely slow growth at ~23 mm, and higher growth rate again below  
523 ~25 mm. Our age-depth modelling approach reproduces the growth history of the top ~23 mm  
524 extremely well but mostly fails to reproduce the U-Th based ages within the oldest part (> ~23 mm),  
525 where only the very upper age error of our approach overlaps with the U-Th results. The reason for this  
526 discrepancy is in the change in the reservoir effect, as seen from the DCF derived from the U-Th based  
527 chronology. As *star* assumes that there is no change in the reservoir effect for the time of the absence of  
528  $\text{CaCO}_3$  precipitation, the offset in the age can be well explained by the reservoir effect change.

529 However, the trend in Mg before the growth stop is already an indication of systematic carbonate  
530 dissolution changes. This is encouraging, as with a better understanding of C systematics within the soil-  
531 karst-cave environment this issue could be potentially resolved in future versions of *star*. In the present  
532 model version, the result evaluation critically depends on informed decisions by the user, based on  
533 knowledge of the local conditions and speleothem morphology.

534 Our approach also suggests the presence of a hiatus in the extremely slow growth section (~23 mm) (Fig.  
535 10a). However, we want to emphasize that this phase of slow growth is understood not to reflect a  
536 deterioration in the local hydrologic conditions, but rather depicts changes in the drip centre and water  
537 flow downwards the flowstone. Thus, no  $\text{CaCO}_3$  was deposited at the location of the flow stone core,  
538 which mimics a growth hiatus (Oster et al., 2009).

539



541

542 **Fig. 10:** a) U-Th based age determinations of stalagmite MC3 (black, Oster et al. 2009; 2010; 2015) and  
 543 the result of the radiocarbon based age-depth model (solid grey line) with uncertainties (dotted grey  
 544 lines). Anchor point was 8.7 ka at 9 mm distance from top of the stalagmite. Grey triangles at the bottom  
 545 represent the depths of radiocarbon measurements. b) Reservoir effect variations over depth with  
 546 respect to the U-Th based age-depth model (black) and after the radiocarbon based one (grey). c)  $\delta^{13}\text{C}$   
 547 (grey) and Mg (black) over depth of stalagmite MC3.

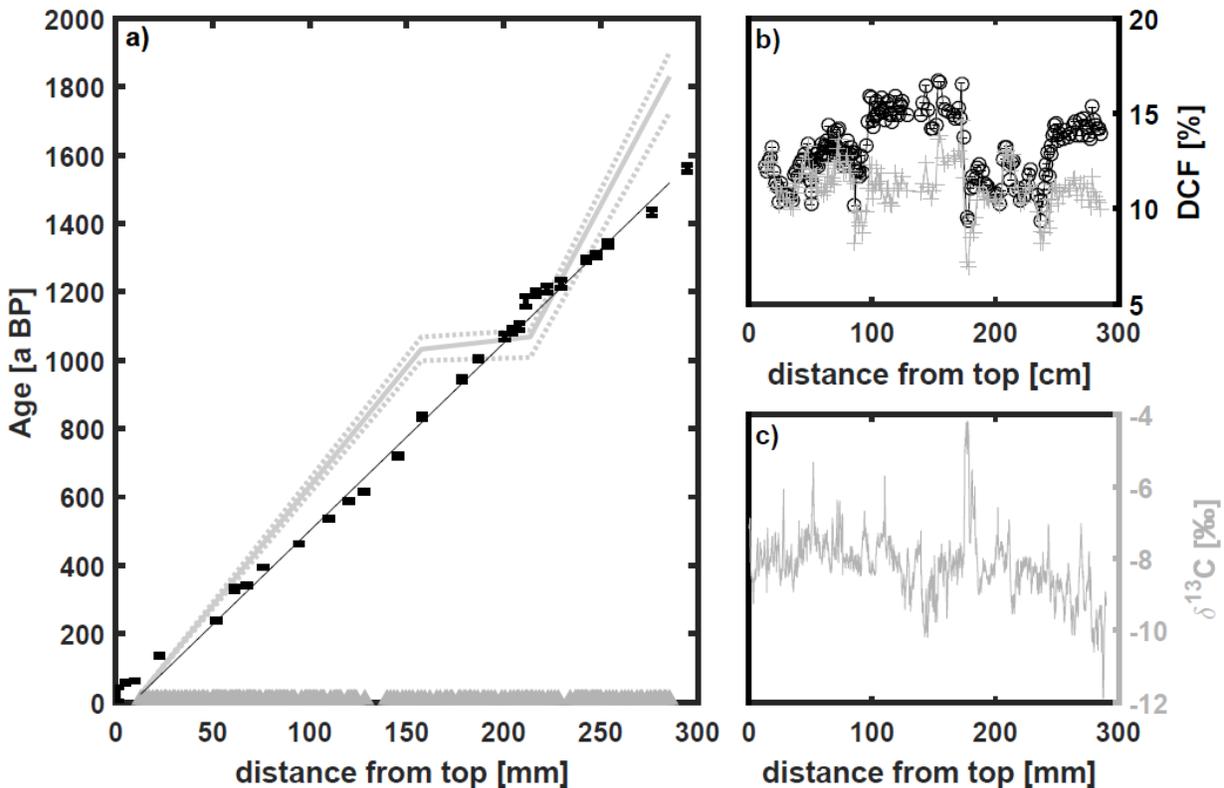
548

549

#### 550 4.4 Stalagmite YOK-I, Yok Balum Cave

551 As a last example, we test *star* on a precisely dated speleothem from Belize (YOK-I, Yok Balum Cave;  
 552 Lechleitner et al., 2016, Kennett et al., 2012). Stable C isotope values (Fig. 10c) and the reservoir effect  
 553 (Fig. 11b) do not show long-term linear trends (Fig. 11c). However, the reservoir effect does show  
 554 secular variations (Fig. 11b), which might be approximated by a polynomial of fourth order. The model  
 555 interprets these variations in the reservoir effect as growth rate variations, resulting in a failed  
 556 reconstruction of the chronology (Fig. 11a). Otherwise, *star* would approximate the U-Th chronology  
 557 well for its linear age-depth result (i.e., before it is searching for growth rate changes).

558



560

561 Fig. 11: a) U-Th based age determinations of stalagmite YOK-I (black, Kennett et al., 2012) and the result  
 562 of the radiocarbon based age-depth model (solid grey line) with uncertainties (dotted grey lines). Anchor  
 563 point was 23 years at 12.8 mm distance from top of the stalagmite, the last radiocarbon measurement  
 564 before the onset of the radiocarbon bomb pulse. The thin black line represents the linear age-depth  
 565 model found by star. Grey triangles at the bottom represent the depths of radiocarbon measurements. b)  
 566 Reservoir effect variations over depth with respect to the U-Th based age-depth model (black, Lechleitner  
 567 et al., 2016a) and after the radiocarbon based model (grey). c)  $\delta^{13}\text{C}$  (grey) over depth of stalagmite YOK-  
 568 I.

569 As the program module for the recognition of growth rate changes uses polynomial remnants of  
 570 reservoir effect variations, the secondary natural DCF variations for YOK-I are interpreted as growth rate  
 571 changes. The positions of the growth rate changes are close to the position with the maximum and  
 572 minimum DCF (determined from the U-Th chronology) at  $\sim 140$  and  $210$  mm distance from top. This  
 573 example illustrates the complexity of our newly included functions with respect to the requirements of  
 574 the stationarity of the radiocarbon reservoir effects. Structured DCF variations can now disturb an  
 575 otherwise reliable age-depth model. However, only this study by Lechleitner et al. (2016) revealed that  
 576 those long-term structures can be implemented in stalagmite radiocarbon reservoir effects. Reservoir  
 577 effect structures, acting on a shorter period of time, will not have any effect on the resulting age-depth  
 578 model.

579

580

## 5. Conclusion

581 We present an improved age-depth modelling approach based on reservoir effect loaded radiocarbon  
582 measurements. The program is now able to detect growth stops, can handle major growth rate  
583 variations and is able to warn the user if the radiocarbon measurements are likely to be subject to  
584 trends in the reservoir effect. The latter point, however, might be regarded as not conclusive as it  
585 represents a trend evaluation after recent knowledge about radiocarbon reservoir effect variability.  
586 More work on C transfer dynamics from the atmosphere to the cave is needed to increase confidence in  
587 this new function.

588 Growth stops can be detected, but need justification by the user. As fast reservoir effect variations can  
589 occur within short periods, an automated mechanism is not applicable. The user should also confirm the  
590 radiocarbon evidence by additional information, e.g., optically visible layers or evidence from  
591 geochemical data. The most important improvement is the detection of phases with different growth  
592 rates. For the present model version, we show that major growth rate variations are more likely  
593 detected. The larger the difference between two consecutive growth rates and the more radiocarbon  
594 measurements are available as well as the more time between phases of different growth rates elapsed  
595 the more likely it is to find phases with different growth rates. The precision of the age-depth models  
596 depends also strongly on the length of the growth period and on the variability of the reservoir effect, as  
597 large scatter in the DCF impede the fitting procedure, or at least result in larger error estimates of the  
598 mean growth rate fit.

599 In summary, this new version of our radiocarbon based age-depth modelling approach can be compared  
600 with age models derived by U-Th dated stalagmites in the early 2000s, when similar piece-wise constant  
601 growth, linear age-depth models were mostly used to describe the growth history of stalagmites.  
602 Realistically, any further improvement of the present-day status of our software would require an  
603 enormous addition of knowledge of C transfer dynamics in karst environments. Such insights would  
604 allow us to implement better options for the evaluation of trends in the radiocarbon reservoir effect,  
605 and to account for them. Even with the recent improvements on *star*, U-Th dating remains the best  
606 option for stalagmite dating when possible, as this method will provide a much better age control.  
607 However, our software provides an option to reliably model the age-depth relationship using  
608 radiocarbon for stalagmites that cannot be dated using U-Th.

609 Finally, we want to mention that *star* is also well applicable to reservoir effect loaded radiocarbon  
610 measurements from other archives, such as ground water aquifers, lake sediments or travertines as long  
611 as the requirements of our approach can be regarded as (nearly) fulfilled.

612

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617 the manuscript.

618

### 619 **Code availability**

620 The code is available on github: <https://github.com/jensfohlmeister/star.git>.

621

622

## 623 **References**

624

625 Bajo, P., Borsato, A., Drysdale, R., Hua, Q., Frisia, S., Zanchetta, G., Hellstrom, J., Woodhead, J., 2017.  
626 Stalagmite carbon isotopes and dead carbon proportion (DCP) in a near-closed-system situation: An  
627 interplay between sulphuric and carbonic acid dissolution. *Geochimica et Cosmochimica Acta* 210, 208-  
628 227.

629 Benavente, J., Vadillo, I., Carrasco, F., Soler, A., Linan, C., Moral, F., 2010. Air carbon dioxide contents in  
630 the vadose zone of a Mediterranean karst. *Vadose Zone Journal* 9, 126-136.

631 Bergel, S. J., Carlson, P. E., Larson, T. E., Wood, C. T., Johnson, K. R., Banner, J. L., Breecker, D. O., 2017.  
632 Constraining the subsoil carbon source to cave-air CO<sub>2</sub> and speleothem calcite in central Texas.  
633 *Geochimica et Cosmochimica Acta*, 217, 112-127.

634 Deininger, M., Fohlmeister, J., Scholz, D., Mangini, A., 2012. The influence of evaporation effects on the  
635 carbon and oxygen isotope composition of speleothems - a model approach. *Geochimica et*  
636 *Cosmochimica Acta* 96, 57-79.

637 Dreybrodt, W., 2008. Evolution of isotopic composition of carbon and oxygen in a calcite precipitating  
638 H<sub>2</sub>O-CO<sub>2</sub>-CaCO<sub>3</sub> solution and the related isotopic composition of calcite in stalagmites. *Geochimica and*  
639 *Cosmochimica Acta* 72, 4712-4724.

640 Dreybrodt, W., Scholz, D., 2011. Climatic dependence of stable carbon and oxygen isotope signals  
641 recorded in speleothems: From soil water to speleothem calcite. *Geochimica et Cosmochimica Acta* 75,  
642 734-752.

643 Fairchild, I. J., Baker, A., 2012. *Speleothem science: From process to past environments*. Wiley-Blackwell.

644 Fairchild, I. J., Treble, P. C., 2009. Trace elements in speleothems as recorders of environmental change.  
645 *Quaternary Science Reviews* 28, 449-468.

646 Fohlmeister, J., Arps, J., Spötl, D., Schröder-Ritzrau, A., Plessen, B., Günter, C., Frank, N., Trüssel, M.,  
647 2018. Carbon and oxygen isotope fractionation in the water-calcite-aragonite system. *Geochimica et*  
648 *Cosmochimica Acta*, 235, 127-139.

649 Fohlmeister, J., Plessen, B., Dudashvili, A. S., Tjallingii, R., Wolff, C., Gafurov, A., Cheng, H., 2017. Winter  
650 precipitation changes during the Medieval Climate Anomaly and the Little Ice Age in arid Central Asia.  
651 *Quaternary Science Reviews* 178, 24-36.

652 Fohlmeister, J., Scholz, D., Kromer, B., Mangini, A., 2011. Modelling carbon isotopes of carbonates in  
653 cave drip water. *Geochimica et Cosmochimica Acta* 75, 5219-5228.

654 Fohlmeister, J., Schröder-Ritzrau, A., Spötl, C., Frisia, S., Miorandi, R., Kromer, B., Mangini, A., 2010. The  
655 influences of hydrology on the radiogenic and stable carbon isotope composition of cave drip water,  
656 Grotta di Ernesto (Italy). *Radiocarbon* 52, 1529-1544.

657 Genty, D., Baker, A., Massault, M., Proctor, C., Gilmour, M., Pons-Branchu, E., Hamelin, B., 2001. Dead  
658 carbon in stalagmites: carbonate bedrock paleodissolution vs. ageing of soil organic matter. Implications  
659 for  $^{13}\text{C}$  variations in speleothems. *Geochimica et Cosmochimica Acta*, 65, 3443-3457.

660 Griffiths, M. L., Fohlmeister, J., Drysdale, R. N., Hua, Q., Johnson, K. R., Hellstrom, J. C., Gagan, M. K.,  
661 Zhao, J.-x., 2012. Hydrological control on the dead-carbon content of a Holocene tropical speleothem.  
662 *Quaternary Geochronology* 14, 81-93.

663 Hua, Q., Cook, D., Fohlmeister, J., Penny, D., Bishop, P., Buckman, S., 2017. Radiocarbon Dating of a  
664 Speleothem Record of Paleoclimate for Angkor, Cambodia. *Radiocarbon* 59, 1873-1890.

665 Hua, Q., McDonald, J., Redwood, D., Drysdale, R., Lee, S., Fallon, S., Hellstrom, J., 2012. Robust  
666 chronological reconstruction for young speleothems using radiocarbon. *Quaternary Geochronology* 14,  
667 67-80.

668 Kennett, D. J., Breitenbach, S. F., Aquino, V. V., Asmerom, Y., Awe, J., Baldini, J.U.L., Bartlein, P., Culleton,  
669 B.J., Ebert, C., Jazwa, C., Macri, M.J., Marwan, N., Polyak, V., Prufer, K.M., Ridley, H.E., Sodemann, H,  
670 Winterhalder, B., Haug, G.H., 2012, Development and disintegration of Maya political systems in  
671 response to climate change. *Science*, 338, 788-791.

672 Lechleitner, F. A., Baldini, J. U. L., Breitenbach, S. F. M., Fohlmeister, J., McIntyre, C., Goswami, B.,  
673 Jamieson, R. A., van der Voort, T. S., Prufer, K., Marwan, N., Culleton, B. J., Kennett, D. J., Asmerom, Y.,  
674 Polyak, V., Eglinton, T. I., 2016a. Hydrological and climatological controls on radiocarbon concentrations  
675 in a tropical stalagmite. *Geochimica et Cosmochimica Acta* 194, 233-252.

676 Lechleitner, F. A., Fohlmeister, J., McIntyre, C., Baldini, L., Jamieson, R. A., Hercman, H., Gasiorowski, M.,  
677 Pawlak, J., Stefaniak, K., Socha, P., Eglinton, T. I., Baldini, J. U. L., 2016b. A novel approach for  
678 reconstruction of accurate radiocarbon-based chronologies for speleothems. *Quaternary Geochronology*  
679 35, 54-66.

680 Minami, M., Kato, T., Horikawa, K., Nakamura, T., 2015. Seasonal variations of  $^{14}\text{C}$  and  $\delta^{13}\text{C}$  for cave drip  
681 waters in Ryugashi Cave, Shizuoka Prefecture, central Japan. *Nuclear Instruments and Methods in*  
682 *Physics Research Section B: Beam Interactions with Materials and Atoms* 362, 202-209.

683 Noronha, A. L., Johnson, K. R., Hu, C. Y., Ruan, J.-Y., Southon, J., Ferguson, J. E., 2014. Assessing  
684 influences on speleothem dead carbon variability over the Holocene: implications for speleothem-based  
685 radiocarbon calibration. *Earth and Planetary Science Letters* 394, 20-29.

686 Noronha, A. L., Johnson, K. R., Southon, J. R., Hu, C., Ruan, J., McCabe- Glynn, S., 2015. Radiocarbon  
687 evidence for decomposition of aged organic matter in the vadose zone as the main source of  
688 speleothem carbon. *Quaternary Science Reviews* 127, 37-47

689 Oster, J. L., Montanez, I. P., Guilderson, T. P., Sharp, W. D., Banner, J. L., 2010. Modeling speleothem  $\delta^{13}\text{C}$   
690 variability in a central Sierra Nevada cave using  $^{14}\text{C}$  and  $^{87}\text{Sr}/^{86}\text{Sr}$ . *Geochimica et Cosmochimica Acta* 74,  
691 5228-5242.

692 Oster, J. L., Montanez, I. P., Santare, L. R., Sharp, W. D., Wong, C., Cooper, K. M., 2015. Stalagmite  
693 records of hydroclimate in central California during termination 1. *Quaternary Science Reviews* 127, 199-  
694 214.

695 Oster, J. L., Montanez, I. P., Sharp, W. D., Cooper, K. M., 2009. Late Pleistocene California droughts  
696 during deglaciation and Arctic warming. *Earth and Planetary Science Letters*, 288, 434-443.

697 Reimer, P. J., Bard, E., Bayliss, A., Beck, J. W., et al., 2013. IntCal13 and Marine13 radiocarbon age  
698 calibration curves 0-50,000 years cal BP. *Radiocarbon* 55, 1869-1887.

699 Rudzka, D., McDermott, F., Baldini, L. M., Fleitmann, D., Moreno, A., Stoll, H., 2011, The coupled  $\delta^{13}\text{C}$ -  
700 radiocarbon systematics of three Late Glacial/early Holocene speleothems; insights into soil and cave  
701 processes at climatic transitions. *Geochimica et Cosmochimica Acta*, 75, 4321-4339.

702 Rudzka, D., McDermott, F., Suric, M., 2012. A late Holocene climate record in stalagmites from Modric  
703 Cave (Croatia). *Journal of Quaternary Science* 27, 585-596.

704 Scholz, D., Frisia, S., Borsato, A., Spötl, C., Fohlmeister, J., Mudelsee, M., Miorandi, R., Mangini, A., 2012.  
705 Holocene climate variability in North- Eastern Italy: Potential influence of the NAO and solar activity  
706 recorded by speleothem data. *Climate of the Past* 8, 1367-1383.

707 Scholz, D., Mühlinghaus, C., Mangini, A., 2009. Modelling  $\delta^{13}\text{C}$  and  $\delta^{18}\text{O}$  in the solution layer on  
708 stalagmite surfaces. *Geochimica et Cosmochimica Acta* 73, 2592-2602.

709 Sinclair, D. J., Banner, J. L., Taylor, F. W., P., J., Jenson, J., Mylroie, J., Goddard, E., Quinn, T., Jocson, J.,  
710 Miklavic, B., 2012. Magnesium and strontium systematics in tropical speleothems from the Western  
711 Pacific. *Chemical Geology* 294, 1-17.

712 Zhang, H., Cai, Y., Tan, L., Qin, S., An, Z., 2014, Stable isotope composition alteration produced by the  
713 aragonite-to-calcite transformation in speleothems and implications for paleoclimate reconstructions.  
714 *Sedimentary Geology* 309, 1-14.